

Grade 12 Applied

Quiz Debrief Week 1

26 Jan 2023

MrF



Most of this should be familiar!

Grade 12 Applied Week 1 Quiz

A quick weekly quiz. Time limited! Open book (obviously). Use my cheat sheet(s) or any notes. Issued '*cheat sheets*' from the other grades are mighty useful!

The quiz will be made available for 90 mins at or before start of class. Submissions will be shut down after 90 minutes.

Have scrap paper and calculator ready.

Read instructions!

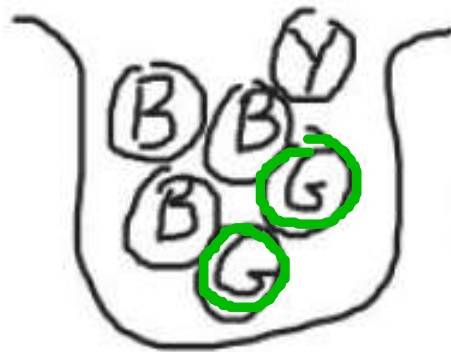
Round all decimal amounts to nearest 0.01. **Simplify** (reduce) all fractions as usual.



Use the notation **cm²**, for example, to represent **square units** of measure since superscript exponents are not practicable in the webpage.

There are several **Bonus** questions if you need the marks. Do them regardless.

Cher has a bag of marbles as pictured below. Determine the theoretical probability that she draws out a **Green** marble. Select best answer. * 2 points



B = Blue
G = Green
Y = Yellow

$$\text{Probability} = \frac{\# \text{ Favoured outcomes}}{\# \text{ all possible outcomes}}$$

4:2 odds

1/2

50%

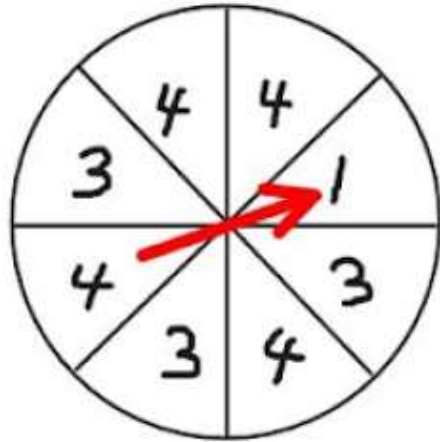
1/3

2/6

$$P(\text{Green}) = \frac{2 \text{ green}}{6 \text{ total}} = \frac{2}{6} = \frac{1}{3}$$

Reduce all fractions

Given the fair spinner below, determine the **probability** that an **outcome** of "4" will be spun on any spin.



"Fair" spinner;
each outcome
equally likely!

Four "4's"

~~4~~ Really? 400%?
~~100%~~ Really?

16%

50% ✓

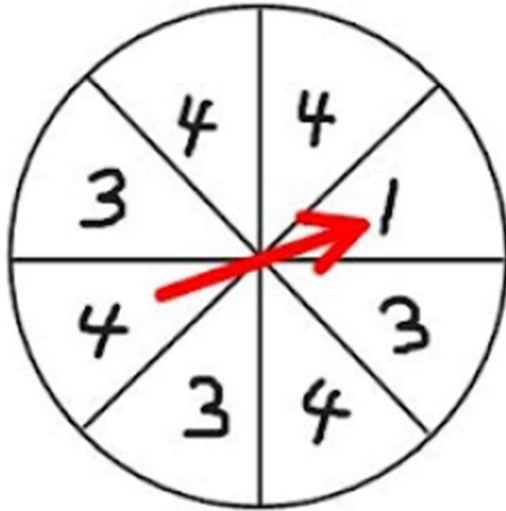
Other:

$$\text{Probability} = \frac{\# \text{Favoured outcomes}}{\# \text{all possible outcomes}}$$

8 possible

$$P(\text{spinning "4"}) = \frac{4}{8} = \frac{1}{2} = 50\%$$

In a game the fair spinner below is spun 440 times. Determine how many times it is **expected** that it will have an outcome of "1".



$$P(\text{spin "1"}) = \frac{\# \text{ Fav OUTCOMES}}{\# \text{ Total possible}} = \frac{1}{8}$$

$$440 \cdot \frac{1}{8} = \frac{x}{\cancel{440}} \cdot \cancel{440}$$

$$x = \frac{440}{8} = 55$$

~~about 10 times unless the ecliptic resonates~~

8 times exactly

~~4.40%~~

55 times

Other:

? Really makes no sense

? don't pick this one! lol

LOL, common sense? The only answer that even comes close to being reasonable is 55 times you can expect to spin a '1'

Grade 10. Solve the proportion below. State your answer.

$$\frac{5}{8} = \frac{x}{20}$$
$$x = ?$$

CROSS MULTIPLY

$$\frac{5}{8} = \frac{x}{20} ; x = \frac{5 \cdot 20}{8}$$
$$x = 12.5$$

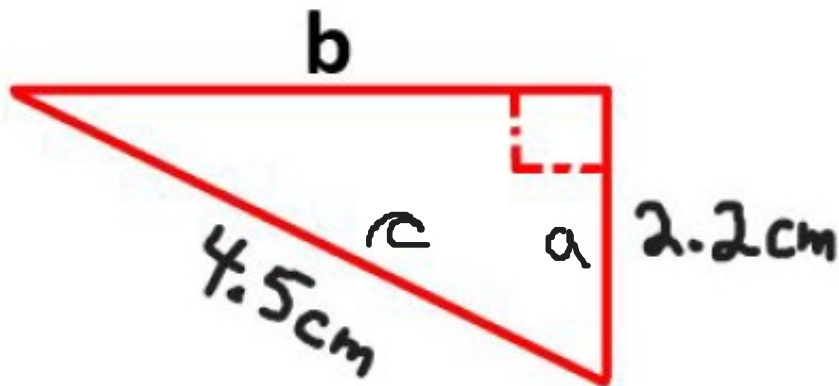
Lazy Algebra

Proper Solution:

$$20 \cdot \frac{5}{8} = \frac{x}{\cancel{20}} \cdot \cancel{20}$$

$$\textcircled{12.5} = \frac{100}{8} = \frac{20 \cdot 5}{8} = x$$

Grade 10. Determine the length of side b. Select the best answer. [Hint: Pythagoras]



$$c^2 = a^2 + b^2$$

$$4.5^2 = 2.2^2 + b^2$$

$$20.25 = \quad \quad b^2$$

$$- 4.84$$

$$b^2 = 15.41 \quad ; \quad b = \sqrt{15.41}$$

= 3.9255572852

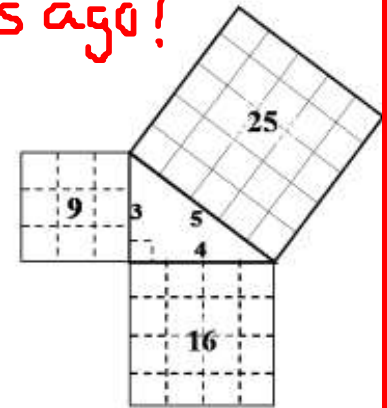
$$; \quad b = 3.93$$

Grade 10

3,000 years ago!

$$c^2 = a^2 + b^2$$

where c is the length of the hypotenuse and a and b are the lengths of the shorter two sides



$$5^2 = 3^2 + 4^2$$

$$25 = 9 + 16$$

or

$$25 - 9 = 16$$

Round properly!!
As instructed

Problem Solve. A farmer has 40 animals, chickens and cows. He forgets how many he has of each but he remembers they have 96 legs all together. How many chickens does the farmer have?

Done these about ten times already

20

idk

32

28

25

8

Multiple Choice!! Just pick the one that works

Hint: Chickens have two legs, cows have 4

WRONG!

$$\cancel{20} \text{ chickens} \cdot 2 \text{ legs/chicken} + 20 \text{ cows} \cdot 4 \text{ legs/cow} \\ = 40 + 80 = 120 \text{ legs} \quad \text{WRONG}$$

$$32 \text{ chickens} \cdot 2 \text{ legs/chicken} + 8 \text{ cows} \cdot 4 \text{ legs/cow} \\ = 32 \cdot 2 + 8 \cdot 4 \\ = 64 + 32 = \boxed{96} \quad \text{Yes! 32 chickens works!!}$$

Problem Solve. A farmer has 40 animals, chickens and cows. He forgets how many he has of each but he remembers they have 96 legs all together. How many chickens does the farmer have?

Guess & Check!

Done these about ten times already

20

idk

32

28

25

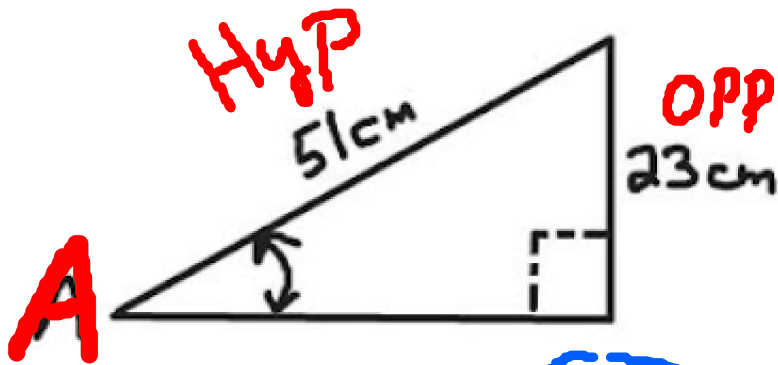
8

	# chickens	chick legs	# cows	# cow legs	Legs Total
	20?	20	$40 - 10 = 30$	$30 \cdot 4 = 120$	120 X
	28?	(40)	20	(80)	(120) X Bzzt
	25?	60	10	40	100 legs
	(32?)	(64)	8	(32)	96 legs ✓

WRONG X?
 Guess again
 WRONG!
 X 30?
 WRONG!
 @lose!

Yes 32 chickens

BONUS 1. [Grade 10, two Bonus marks if you need them]. Determine the measure of Angle A in degrees. State it below.



Your answer

SOH CAH TOA

$$\sin \angle A = \frac{\text{OPP}}{\text{Hyp}} = \frac{23}{51}$$

$$\angle A = \sin^{-1} \left(\frac{23}{51} \right) = 26.81^\circ \text{ TLAR!}$$

$$\sin^{-1} \left(\frac{23}{51} \right)$$

$$= 26.80660230$$

Grade 10 Trig

Unit E - Trigonometry

SOH CAH TOA. $\sin A = \frac{\text{side opp to } \angle A}{\text{hypotenuse}}$; $\cos A = \frac{\text{side adjacent to } \angle A}{\text{hypotenuse}}$; $\tan A = \frac{\text{side opp to } \angle A}{\text{side adj to } \angle A}$

$\sin A = \frac{a}{c}$ $\sin B = \frac{b}{c}$
 $\cos A = \frac{b}{c}$ $\cos B = \frac{a}{c}$
 $\tan A = \frac{a}{b}$ $\tan B = \frac{b}{a}$

$\cos \theta = \frac{\text{Adj}}{\text{Hyp}} = \frac{4}{7} \approx 0.5714$
 $\theta = \cos^{-1} \left(\frac{4}{7} \right) \approx 55^\circ$

Hypotenuse side is always across from the 90° corner.
 If know two parts of a right triangle, can figure out the rest.
 Handy rule: longest side across from biggest angle, smallest side across from smallest angle.
 Round trig ratios to nearest 0.0001 normally

To find measure of angle:

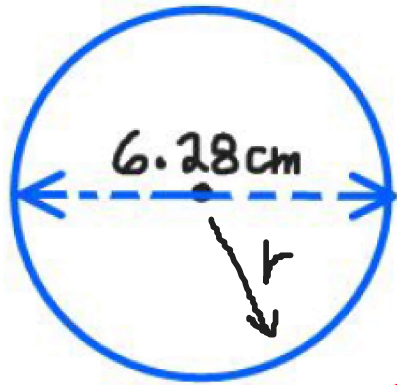
$\theta = \tan^{-1} \left(\frac{2}{4} \right)$
 $\theta = \sin^{-1} \left(\frac{2}{4} \right)$
 $\theta = \cos^{-1} \left(\frac{4}{4} \right)$
 $\theta = 26.57^\circ$

To find a side:

$\cos 30^\circ = \frac{4}{x}$
 $\cos 30^\circ = \frac{4}{x}$
 $x = \frac{4}{\cos 30^\circ}$
 $x = 4.62 \text{ cm}$

Several cheat sheets
 Show you

Bonus 2. [Grade 10] Determine the **Area** of the circle and select the answer below.



30.97 cm²

~~123.98 cm²~~

~~19.73 cm³~~

~~39.44 cm~~

→ doesn't make sense?

~~x~~ cm³ is Volume, not area lol.

~~x~~ cm is length not area!

The only logical answer!

But

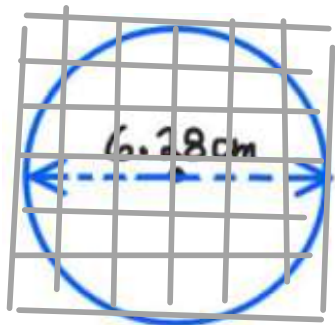
$$A_{\text{circle}} = \pi \cdot r^2$$

$$A = \pi \cdot (3.14 \text{ cm})^2$$

$$A = 30.97 \text{ cm}^2$$

$$\pi \cdot 3.14^2$$

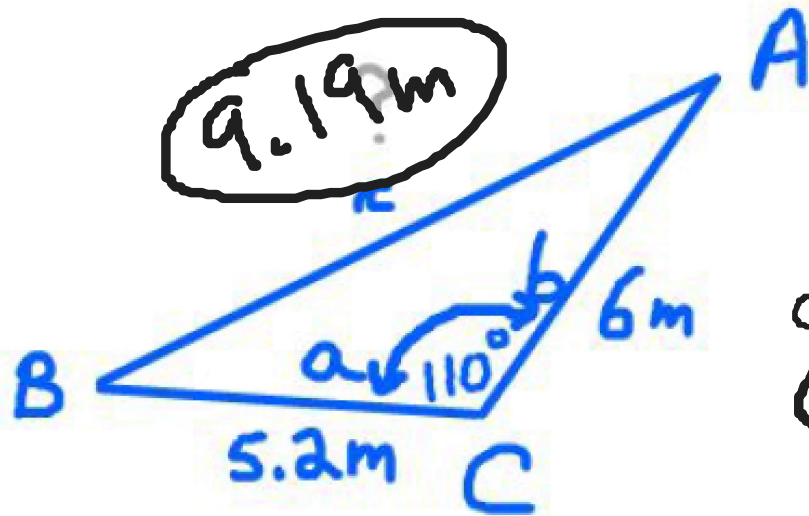
$$= 30.9748469$$



Got to be less than 36 squares? Logic?

Bonus 3. [Grade 11] Go real crazy with the Cosine Law. Solve for side 'c'.
State the answer below.

Fun!



$$c^2 = a^2 + b^2 - 2 \cdot a \cdot b \cdot \cos(C)$$

$$c^2 = 5.2^2 + 6^2 - 2 \cdot 5.2 \cdot 6 \cdot \cos(110^\circ)$$

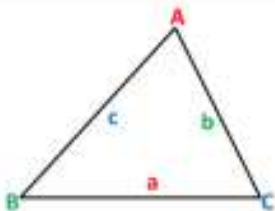
$$c = 9.19 \text{ m}$$

$$5.2^2 + 6^2 - 2 \cdot 5.2 \cdot 6 \cdot \cos(110)$$

$$= 84.382056943$$

$$\sqrt{84.38205}$$

$$= 9.1859702808$$



Gradell

Trigonometry Cosine Law:

Cosine Law for *side a* across from angle A: $a^2 = b^2 + c^2 - 2 \cdot b \cdot c \cdot \cos(A)$

Cosine Law for *angle A* given three sides: $\cos(\angle A) = \frac{b^2 + c^2 - a^2}{2bc}$ or $\angle A = \cos^{-1}\left(\frac{b^2 + c^2 - a^2}{2bc}\right)$

Various arrangements of formula: $a^2 = b^2 + c^2 - 2 \cdot b \cdot c \cdot \cos(A)$

$b^2 = a^2 + c^2 - 2 \cdot a \cdot c \cdot \cos(B)$; or $c^2 = a^2 + b^2 - 2 \cdot a \cdot b \cdot \cos(C)$