GRADE 10 ESSENTIAL
UNIT D – 2D GEOMETRY

CLASS NOTES

INTRODUCTION

1. How much paint do you need to paint your bedroom? How many paving stones do you need to buy to make your aunt's garden patio? How many boards do you need to buy to make your child's sand box.

2. These type of questions are frequent in your life. Of course as a helpful spouse, nephew/niece, or parent it is your job to know how to calculate the answer to these types of everyday problems.

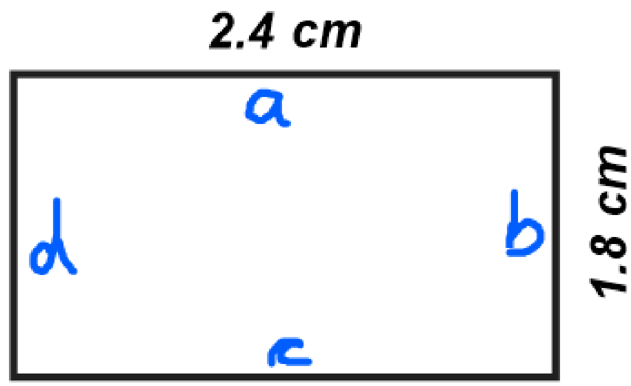
3. In this unit we learn about area and perimeter of flat two-dimensional shapes. Much of this may be a worthwhile refresher from previous studies.

PERIMETER

4. **Perimeter of a Rectangle**. Perimeter is the total distance around the outside edge(s) of a flat object. The *perimeter* highway goes around the city! '*Peri*' means close or around; '*meter*' means measure in ancient languages.

5. What is the distance around this rectangle →.

This is just a picture of the problem so it likely is not the real measurement. But what is the unknown value of the perimeter; let's call it '**P**'.



caution: not drawn to scale, not necessarily the correct measurement, do not actually measure it with a ruler!

6. Value of the **P**erimeter equals length **a** *plus* length **b** *plus* length **c** *plus* length **d**.

or more concisely: **P = a + b + c + d**

7. There is **your first geometric formula** (**!**), the perimeter, **P**, of this four-sided figure with straight sides (ie: a *quadrilateral*) is **P = a + b + c + d;** *where a, b, c, and d are the lengths of the sides. "What is a quadrilateral ?", you might ask: Check the glossary the end of these notes or just google it for yourself.*

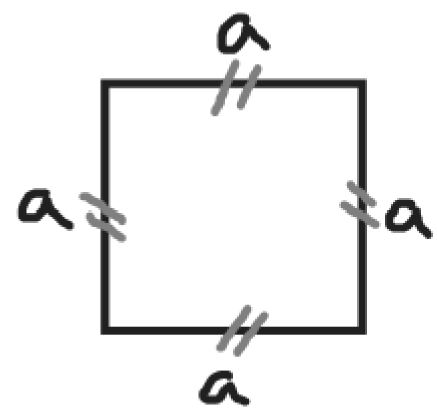
8. *But wait*!! Sides **a** and side **c** the same length! And sides **b** and **d** the same length too? So why not give them the same letter if their values are the same? So, we could say:

P = a + b + a + b; *or you could say:*
P = 2a + 2b; *or you could say:*
P = 2 (a + b)*;*
where and b are the lengths of opposite sides.

Pretty fancy formulae to calculate the distance around a rectangle!

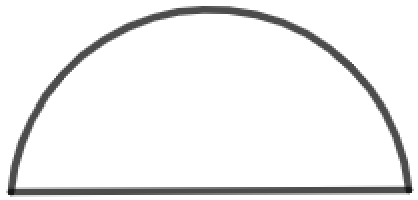
Perimeter of a Square

9. A square is a particular rectangle in which all the edges happen to be the same length. So, we give them the same symbol for the value of the length of the edge, **a** in this case.



*some books call the '**a**' an '**s**' for side. Does it matter what letter you give it?*

P = a + a + a + a; *or*
P = 4*a

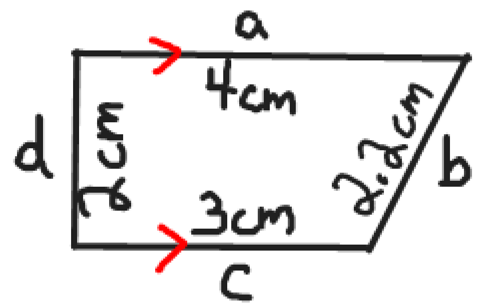


10. Shapes can have three to any number of sides. Sides can be straight edges (polygons) or even irregular shaped edges (circular). See the Appendix to these notes for a refresher on the naming of shapes.

← This is a semicircle, a straight line segment with a circular arc formed by a half circle.

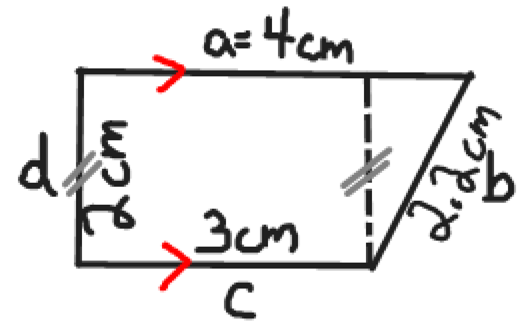
Perimeter of a Trapezoid

11. A trapezoid is a 4-sided polygon (ie: a quadrilateral) where one pair of sides are parallel. Notice the arrow head indicated the pair of sides that are going in the same direction.

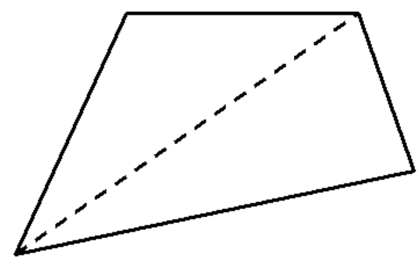


P = a + b + c + d

12. **Perimeter of a Triangle**. Did you notice that a trapezoid is really a rectangle with a triangle stuck on one end (could even be two ends)



Triangles are magic! Every shape can be made of triangles. We therefore must do an extensive study of triangles shortly.

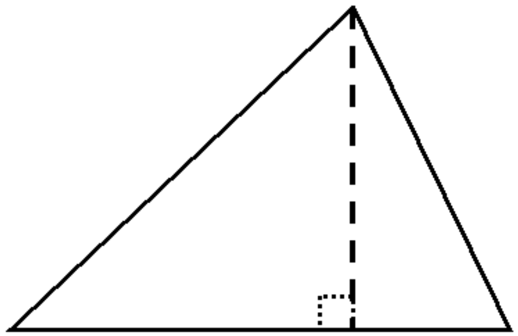


13. A triangle is a polygon with three angles. ['*tri*' + '*angle*']. Consequently, it has three sides as well.

You might recall all the different kinds of triangles. → It is certainly worthwhile to know the names of things you work with!

Types of Triangles	
Based on angles	**Based on comparing sides**
right	equilateral
acute	isosceles
obtuse	scalene

15. Regardless of the types of triangles, the **most important triangle** is the **right triangle**. *Every* kind of triangle can be made of two right triangles and every shape can be made of some triangles, it is important to be rather familiar with a right triangle especially and all its magic.



THE 'RIGHT' (90 DEGREE) TRIANGLE

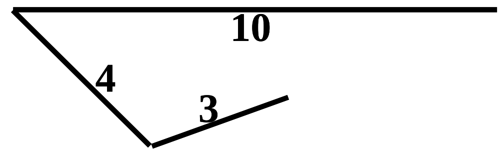
16. We will start to study the right triangle now. If you understand the right triangle you seriously understand every polygon shape in the universe. Every polygon can be made of triangles. Even circles can be made of triangles!

Pythagorean Theorem (The Law of Pythagoras)

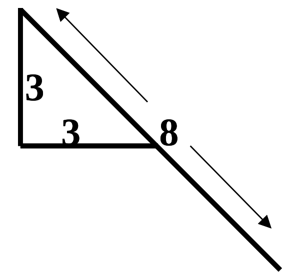
This is very important! If there were 10 things you just had to know about mathematics for the rest of your life this is one of them for sure.

17. **Experiment 1**. Take three different length slurpee straws or strips of paper and try to make a triangle of any kind by connecting the ends of those lengths. You might find there are some combinations of lengths that cannot make any triangle!

a. Try a **10**, a **4**, and a **3**. It doesn't work. The 10 is too long

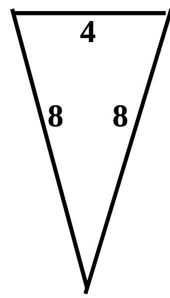


b. Try a **3**, a **3**, and a **8**. It doesn't work. The 8 is too long.



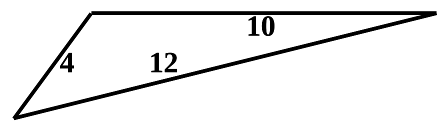
c. But a **8**, a **8**, and a **4**, does work. What kind of triangle is it though??

____



d. Try a **10** a **4** and a **12**, it works. What kind of triangle is that?

____



It turns out, as you may have figured out, that the sum of any two sides of a triangle has to be longer than the third remaining side! Investigate on your own the 'Triangle Inequality Theorem'

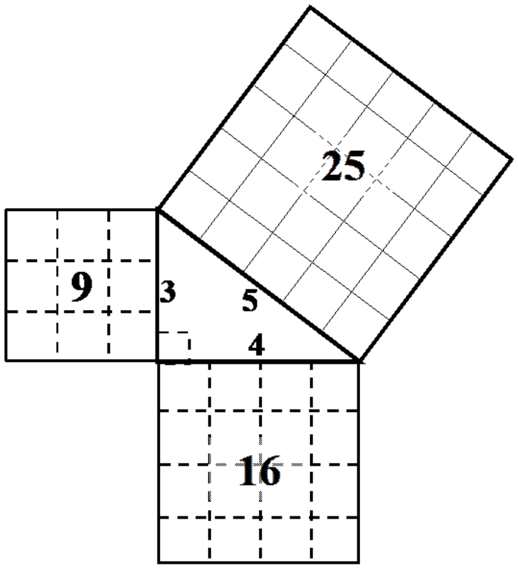
18. **Experiment 2**. Take three different length slurpee straws or slips of paper and try to make a right triangle! This will be very difficult. How can it be so difficult if there are right triangles everywhere??!!

Obviously, there is some **secret** to making right-triangles.

19. **Pythagorean Theorem**. One of the more ancient and critical concepts of all. Many cultures had discovered 2500 years ago that "***given any right-triangle, the square on the longest side equals the sum of the squares on the other two sides***". The law has the Greek mathematician Pythagoras's name because he proved it and recorded it. But ***ancient bead work*** in some North American indigenous cultures suggests they knew it too.

This is one of those math concepts you really do need to know for the rest of your life! Honestly!

It's a law!



20. Given **any** right-triangle: "the square on the longest side equals the **sum** of the squares on the other two [shorter] sides."

In '*algebraic*' form:

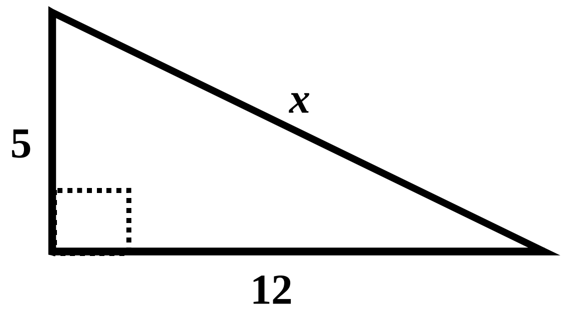
$c^2 = a^2 + b^2$; ******where *c* is the longest side****** ***c*** is <u>*alone by itself*</u> in the equation!!!!!! ****

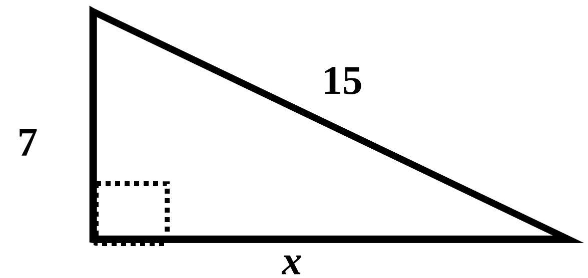
The longest side is called the ***hypotenuse*** and is **always *across*** from the **right angle**.

21. You most definitely need to add this idea to your two-page cheat sheet [Study Notes]

Pythagoras Examples: *You try*!

22. Given the two right-angle triangles below; find length ***x***. (The triangles are **not** '*drawn to scale*', so you can't just measure them!)

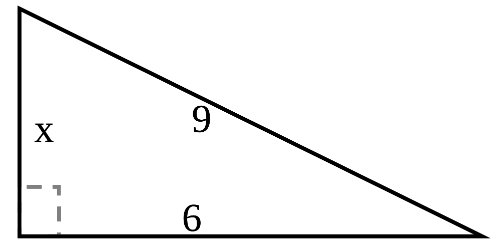




Ans: 13 exactly

Ans: ab*out* (~) **13.27** if you round to two decimal places.

WORKED EXAMPLE - PYTHAGORAS



23. The more difficult problem is to **find a short side** when you are given the other short side and the hypotenuse.

Write down the formula (*you only have one!*)

$c^2 = a^2 + b^2$; now plug in the numbers in the correct place; (*'c' is the hypotenuse in this formula!*)

$9^2 = 6^2 + b^2$ evaluate the squared numbers

So **$81 = 36 + b^2$** ; get the b^2 by itself

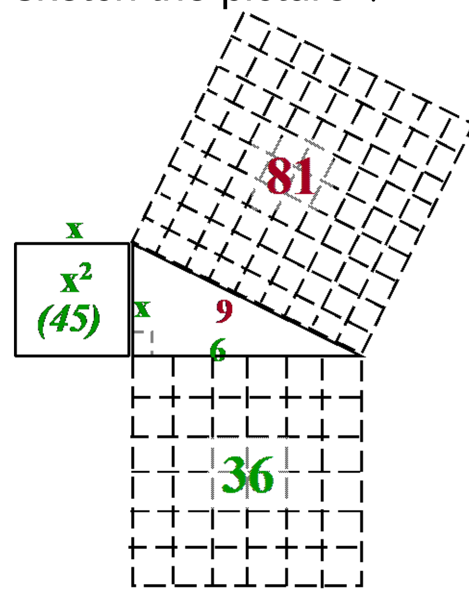
$81 – 36 = b^2$; evaluate (subtract)

$45 = b^2$; now calculate the 'b' by 'unsquaring'

6.7082… = b

∴ **b = 6.71** rounded to nearest hundredth

If you don't like all the fancy steps to the left (algebra) just sketch the picture ↓



Square and Square Roots of Numbers

25. If you are not overly familiar with the idea of squares and square roots from previous studies try this quick lesson; complete the table here:

x →	**2**	**3**	**8**			**5**		$\leftarrow \sqrt{y}$
x^2 →				**81**	**100**		**49**	$\leftarrow y$

Evaluate the following squares and square roots (to nearest hundredth; 0.01)

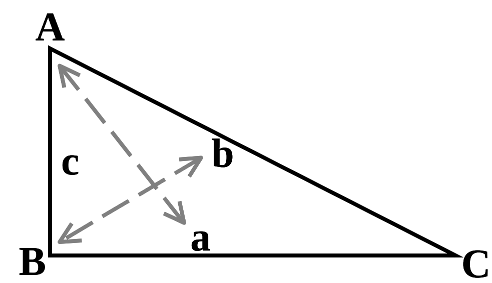
a. $\mathbf{2.5^2}$	b. $\sqrt{6.25}$	c. $\mathbf{7.071^2}$	d. $\sqrt{50}$
e. $\mathbf{100^2}$	f. $\mathbf{1000^2}$	g. 7.1^2	h. $\sqrt{7.1^2}$

I almost alway guess before I use calculator

Labelling Triangles (*special way*)

As usual CORNERS are labelled with CAPITAL LETTERS and sides are labelled with small letters.

But triangles have **special labelling**; the small letter across from a corner is the same as the CAPITAL letter at the corner across.



You may recall that side '**a**' can also be called side $\overline{BC}$**.** You may see it labeled in that manner occasionally

Un-natural Numbers (Irrational Numbers)

26. Often when doing a square root you will end up with a crazy number on your calculator like:

$\sqrt{5} = 2.236067977$. It actually turns out to be closer to **this** really →

2.2360679774997896964091736687313……………; *(however it goes on forever with no pattern);* but **your** calculator display is too small to show it all so it rounds it off after 8 or so decimal places!

So normally you would just properly round the answer to 2 or 3 decimal places as directed in an assignment.

PERIMETER OF A CIRCLE (CIRCUMFERENCE) AND π

27. **The Circle**. Another rather important shape! The circle. Another important formula that you should have memorized forever. Seriously!

28. **Experiment**. Make a good circle. Measure the distance across the centre of the circle, call it **d** for diameter. Measure the distance around the circumference of the circle, call it **C** for circumference. Calculatethis: **C ÷ d**; or since we are in high school now more properly written **C/d**.

It doesn't matter what you use for units of measure; cm, mm, inches; miles; ….

Your answer had best come out close to a **bit more than 3**. If it did not the universe is collapsing.

30. The real value of **C/d** for any and for all circles is:

3.1415926535897932384626433832795…→

We call this number '**Pi'** and use the Greek alphabet symbol 'π'.

31. There is a button on your calculator that will tell you the value is **3.14159265** (depending on the precision of your calculator display). Find the π on your calculator.

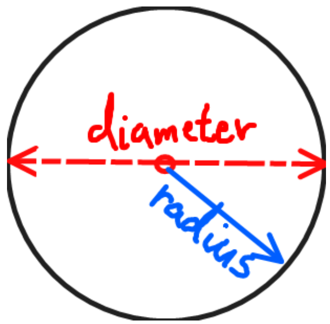
32. If we are doing manual calculations without a calculator we usually just use **3.14** as a close decimal *approximation* to π. The fraction **22/7** works nicely two if, like me, you prefer fractions.

π is another one of those pesky numbers that has decimal places that go on and on forever with no rational pattern! It is '***irrational***'. Mathematicians have calculated it recently to six trillion decimal places, we will tend to just stick with whatever the calculator tells us or sometimes just 3.14.

35. **Calculate the Circumference**. Circumference is a specific word for a **perimeter** of a circle. The formula for circumference is:

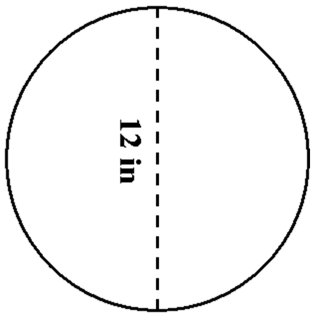
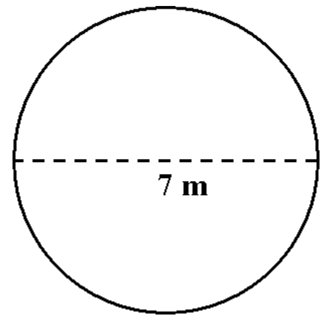
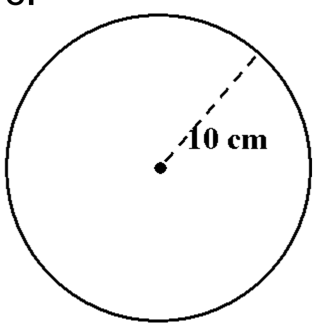
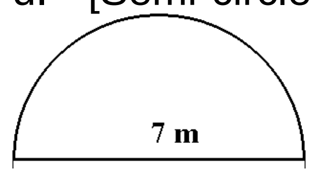
36. Circumference equals π times diameter; or **C = π•d** , where '**d**' is the diameter. Also recall that a radius 'radiates' from the centre of a circle to the circumference, so a diameter cutting across the centre of the full circle is really the same length as two radii.

Distance around a circle (**Circumference**)
Circumference is really a perimeter, but a different word is used for circles.



C = 2πr; where r is the radius measurement
or since **2*r** is a diameter; or
C = πd where **d** is the diameter measurement.

37. **You Try**; calculate the perimeter (circumference) of the following: (round to nearest hundredth decimal place as usual unless otherwise specified):

a. 	b. 
c. 	d. [Semi-circle] 
e. A donut with a radius of 14.2 cm.	f. A pizza with a diameter of 14”

Working a Formula

40. If you already know the circumference but want the diameter, the formula still works, it just needs to be juggled around a bit. **Example**: You know the circumference of a bike wheel is 70 inches, what is its diameter?

a. **Solve by Simple Proportion**. You know that a wheel of 1 unit in diameter is 3.14 units of circumference, so:

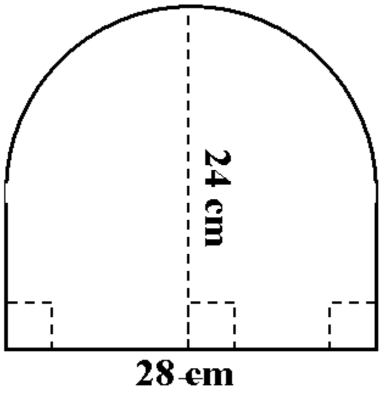
$$\frac{1}{3.14} = \frac{d}{70}; \quad \therefore \text{ d} = \frac{70}{3.14} = 22.29\ in$$

b. **Solve by algebra**. Math students learn to more quickly manipulate symbols to solve problems using '*algebra*'.

if **C = 3.14* d** but you want to know just '**d**' when you are told the **C**, then '*un-multiply*' (ie: divide) both sides of the formula by the 3.14 to find the '**d**' by itself.

If **C = 3.14* d ,** then the 'new' formula to calculate **d** is: $d = \frac{C}{3.14}$**.** It is still the same relationship, just re-arranged, much like saying: "my sister is twice my age; so I am half her age".

Perimeter of Irregular Shapes 1.



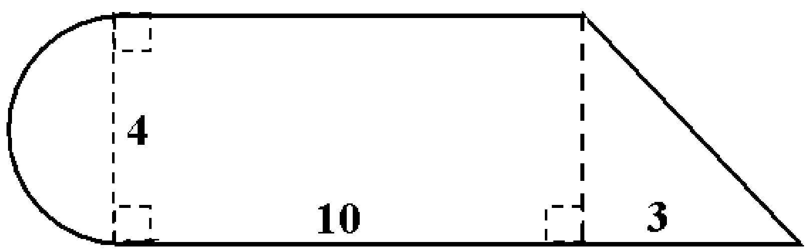
41. Not every shape you encounter is a nice easy shape. Some shapes are combinations of several shapes.

42. Say you are designing a plaque to award the top student. It is a rectangle with a semi-circle on top. You want to put a gold ribbon around the entire perimeter. What length of gold ribbon do you need? **[SHOW WORK]**

Ans: 91.96 cm

Perimeter of Irregular Shapes 2

43. What is the perimeter length of this irregular shape below?



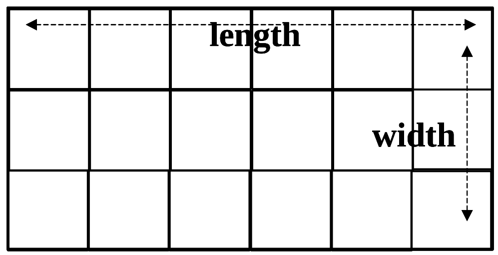
Ans: 34.28 units

AREA OF 2 DIMENSIONAL SHAPES

44. Say you want to paint your child's bedroom walls! You select the perfect colour that she likes. The can says that a one litre can of paint will cover 12 square metres of wall surface. How many litres of paint do you need to buy?

This section is all about **area of shapes**. How much surface they have measured in little unit **squares**.

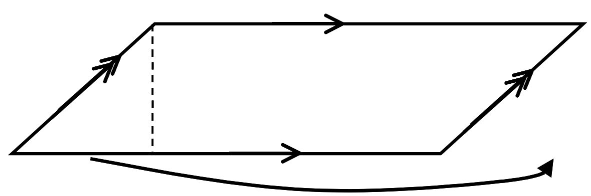
45. **Area: Rectangles and squares**



Area = l * w

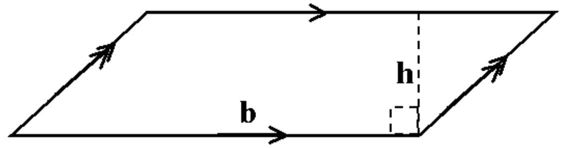
This area is 6 units* 3 units = 18 **square units** or **18 units^2**

46. **Area: Rhombus and Parallelograms**



At right is a parallelogram. Notice how you could rip off the triangle on the left side and add it too the figure on the right side and have a nice easy **rectangle**. The area would not change!

47. Instead of length times width now, we call the area the ***base times the height***.

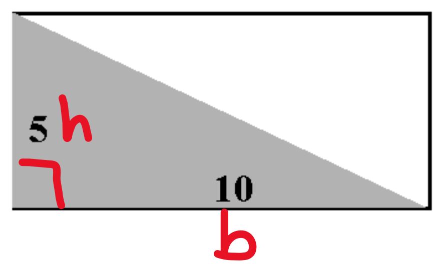


A = b * h;

but notice the '**h**' must be measure perpendicular, at 90 degrees to the base!

48. **Area: [Right] Triangles**

What is the area of the **rectangle** at the right?



__________ square units

Fancy formula for area of half a rectangle:

____

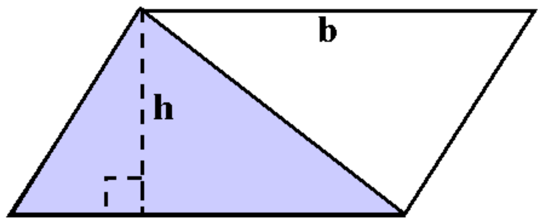
$A_{\Delta} = \frac{1}{2} \cdot b \cdot h$

Did you notice that a [right] triangle is really half of a rectangle?

So, what is the area of the **triangle**? _________

49. **Area: Any Triangle**
(obtuse, right, acute)

What is the formula for the area of the parallelogram at the right?



A = __________

A_Δ = ½ * b * h

Did you notice that ***any*** triangle is really half of a parallelogram?

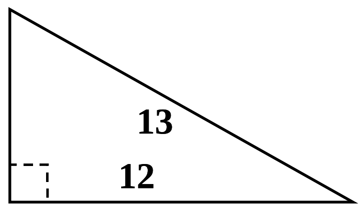
*** '***h***' , height, is always ⊥ to base***

So, what is the area of any triangle?

A = _________

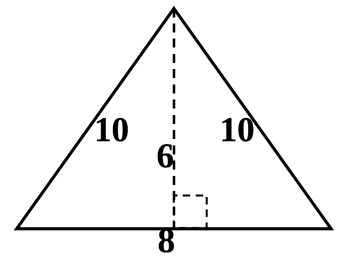
50. Calculate the area of the triangles below: (all indicated measurements are in cm)
****Not to scale!**** *SHOW YOUR WORK!*

a.



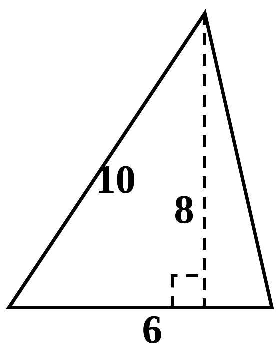
Ans: 30 cm^2

b.



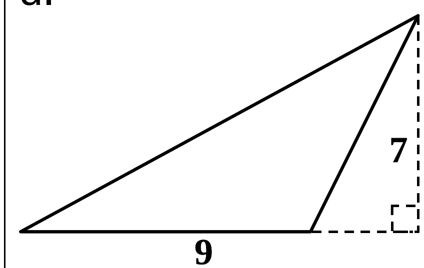
Ans: 24 cm^2

c.



Ans: 24cm^2

d.

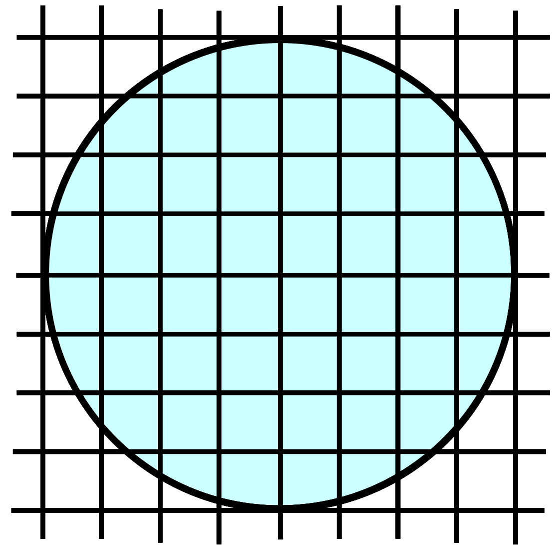


Ans: 31.5 cm^2

Area of a Circle

60. How many squares fit inside a circle? You just **know** that 3.14 is involved somehow!

Count, roughly, how many whole or equivalent little unit squares are inside this circle. Include bits of squares too.



Number of squares (approx?) = ____________

What is the diameter, **d**, of this circle?

____

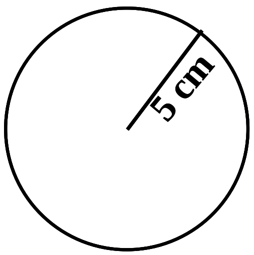
Try this formula: $\mathbf{A = \pi * r^2}$ = ____________

61. So that is the area of a circle!

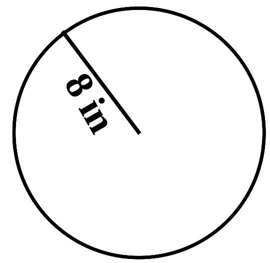
$\mathbf{A_{circle} = \pi * r^2}$; where '**r**' is the radius of the circle. Neat how the ancients figured that out thousands of years ago!

62. Calculate the area of each circle below; use as accurate as value of π as you can. Round final answers to two decimal places.

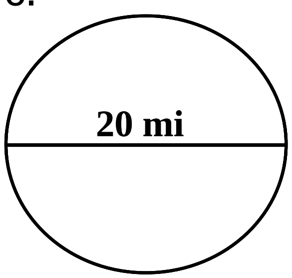
a.



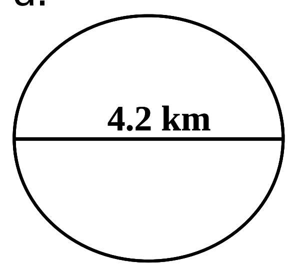
b.



c.



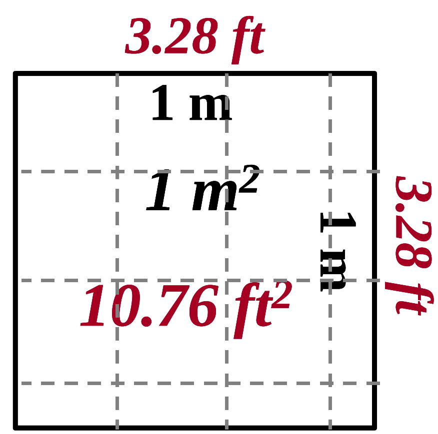
d.



CONVERTING SQUARE MEASURES

65. What if you are painting your son's bedroom and you measure the walls to have an area of 360 square feet [**360 ft²**]. You get to the hardware store and the paint can says it covers 10 square meters [**10 m²**]. How do you convert? How many square meters is the same as how many square feet.

66. Draw a diagram to see the problem! →



See how one square metre is really 10.76 square metres!

1m² = 10.76 m²

Of course, you knew this because you knew that one metre was the same as 3.28 ft.

67. So a metre times a metre, 1 square metre, must be 3.28 ft * 3.28 ft; or what we call **3.28^2 ft²**; ~**10.76 ft²**

So, the rule is you need to convert the length *and* the width into the new units, so you have to do a double conversion; for each edge.

70. You try

a. Convert 16 square yards into square ft

b. Convert 10 square meters into square cm.

Ans: 144 ft^2

Ans: 100,000 cm^2

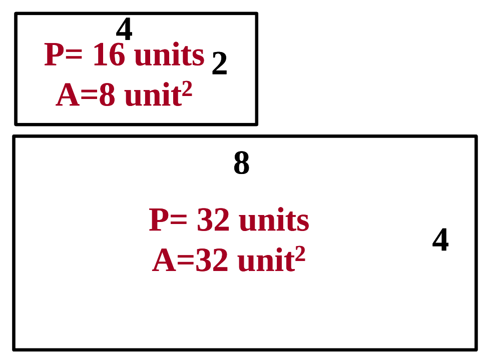
SCALING OF SHAPES

71. What happens to the perimeter and the area of a shape if you just double al the lengths? Check it out! Draw yourself a simple example:

72. Notice that doubling all the lengths doubles the perimeter!

But

Doubling all the lengths also quadruples the area.



73. See why from the geometric formula:
$P_{small} = a + b + c + d$
$\mathbf{P_{big}} = 2a + 2b + 2c + 2d = 2*(a + b + c + d) = \mathbf{2*\ P_{small}}$
but
$A_{small} = b * h$
$\mathbf{A_{big}} = 2*b*2*h = 2^2*b*h = 4bh = \mathbf{4*A_{small}}$

SCALE

74. Scale is a comparison of the lengths of similar shaped objects in some ratio. Big : Little or $\frac{Model}{Actual}$; etc. Doubling the scale doubles the perimeter but quadruples the area. Tripling the scale will change the perimeter by three times but the area by nine times ($3^2 = 9$).

75. Doubling the height and the width of Mona's picture gives her **twice** the **length** of hair, twice the length of nose, twice her hat size around her circumference of her head; etc ***but …..***

doubling the height and the width of Mona's picture gives her **four times the area** of her face (for makeup), four times as much fabric for her blouse, etc.

Think about it!

Mona 1

Mona 2

CONCLUSION

78. That completes your study of the geometry of two-dimensional objects!

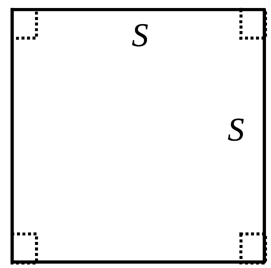
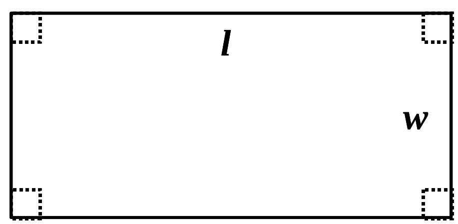
79. You will be given all the necessary geometric formulae on tests and exams (although they are rather logical and can readily be memorized or derived without reference to a formulae sheet)

80. Start to add some of these ideas to ***your*** Grade 10 Reference Notes ('cheat sheet').

81. In Grade 11 you will do three dimensional objects like cubes and cones!

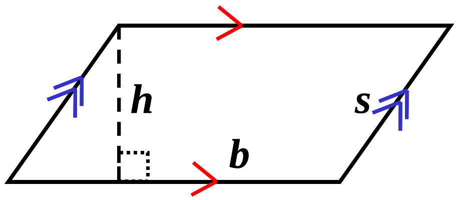
APPENDIX A
GRADE 10 ESSENTIAL
UNIT D – 2-D GEOMETRY

GEOMETRIC FORMULAE

Shape	Diagram	Formulae
	FLAT OBJECTS **2 DIMENSIONAL**	
Square (all four sides same length, 90°corners) (a rectangle with all sides same length)		**Perimeter, P**: **P = s + s + s + s = 4*s** **Area, A:** **A = s * s = s^2**
Rectangle (Four sides, square corners)		**Perimeter, P:** **P = *l* + *w* + *l* + *w* = 2*l* + 2*w*** **Area, A:** **A = *l* * *w***

Parallelogram and Rhombus

(a leaning rectangle or leaning square)
Note
b is always ⊥ to h



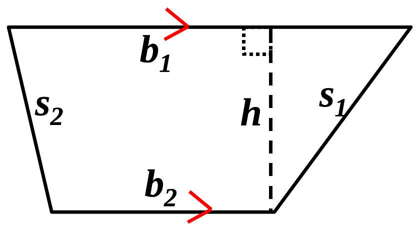
Perimeter; P:
P = 2b + 2s

Area; A:
A = b * h
Note
b is always ⊥ to h

Trapezoid

(Four sides,
only two sides parallel { || })

Note
b is always ⊥ to h



Perimeter; P:
$P = b_1 + s_1 + b_2 + s_2$

Area; A:
A = $b_{avg} * h$

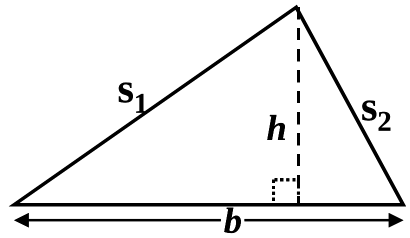
$= \frac{1}{2}(b_1 + b_2) * h$

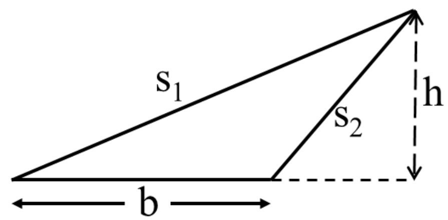
Note
b is always ⊥ to h

Triangle
(three sides)

(half a parallelogram or half rectangle)

Note
b is always ⊥ to h



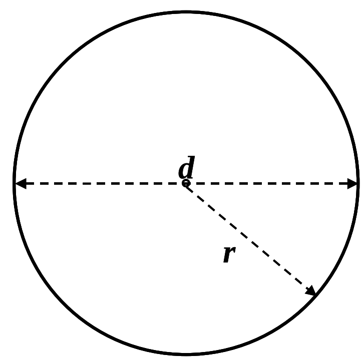


Perimeter; P:
P = $s_1 + s_2 + b$

Area; A:

A = $\frac{1}{2} * b * h$
Note
b is always ⊥ to h

Circle



Circumference; C:

C = $\pi d = 2\pi r$

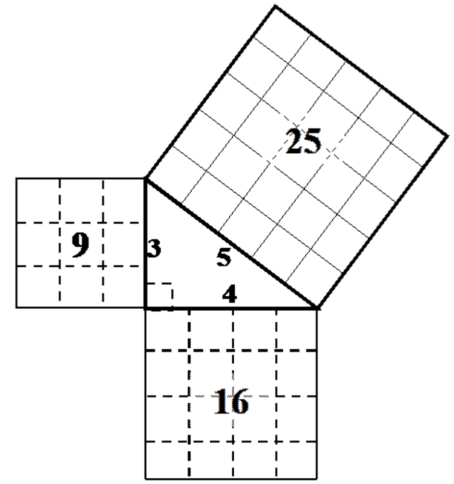
Area; A

A = πr^2

Pythagoras

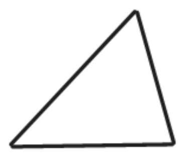
$$c^2 = a^2 + b^2$$

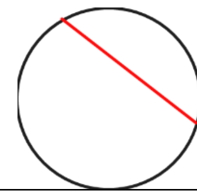
*where **c** is the length of the hypotenuse and **a** and **b** are the lengths of the shorter two sides*

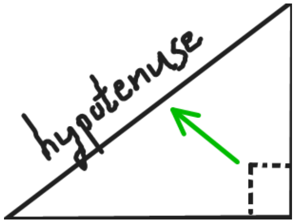


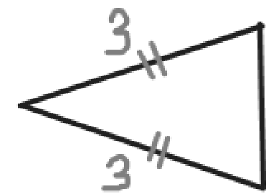
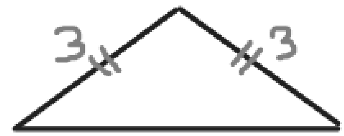
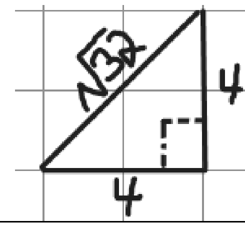
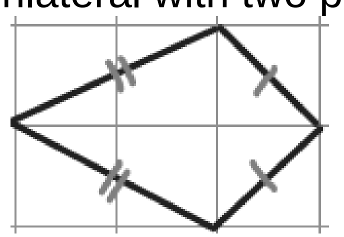
Add your own extra formulae below.

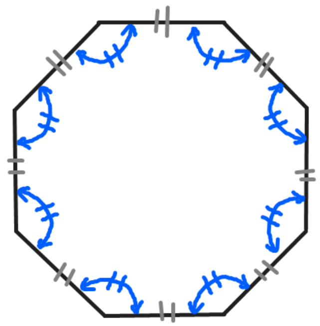
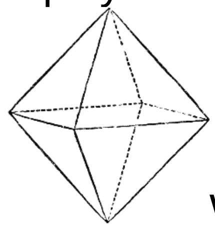
APPENDIX B
TO GR 10 ESSENTIAL
UNIT D – 2D GEOMETRY

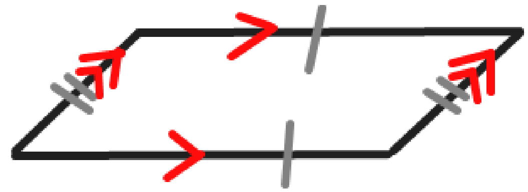
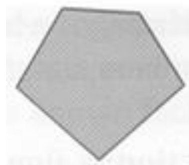
GLOSSARY **(or check Google if not here!)**	
acute angle	an angle measuring less than 90°
acute triangle	a triangle with three acute angles 
algebra	the manipulation of values, variables, and expressions in a formula to solve a problem using very basic and logical rules.
altitude	the perpendicular distance from the base of a figure to the highest point of the figure. Also, the height of an object above the earth's surface.

approximation	a number close to the exact value of a measurement or quantity. Symbols such as ~, ≈ or ≅ or ≑ are sometimes used to represent approximate values.
chord	A line segment with ends on the circumference of a circle. 
congruent:	figures that have the same size and shape, but not necessarily the same orientation.
decagon	a polygon with ten sides.
diameter	distance across a circle (a chord through the centre). A **diameter** is just twice the measure of the **radius** which is measured only from the centre to the circumference.
equiangular polygon	a polygon where all the angles have the same measure. Also known as a **regular** polygon.
evaluate	substitute a value for each of the variables in an expression and simplify the result. (as opposed to solve). Eg: find the value of the expression '2*x* + 1' if the *x* is worth 3. Ans: 7

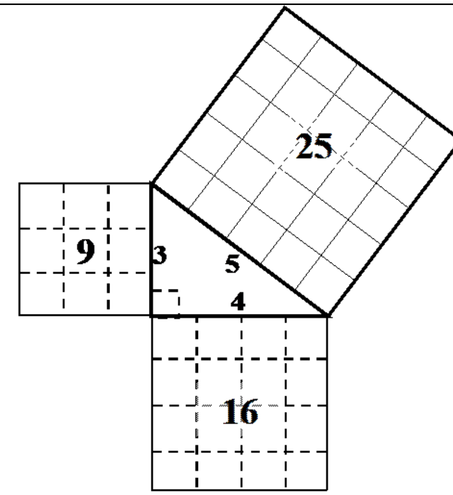
Formula	a mathematical rule that is expressed as an equation to find values of quantities. *Plural*: formulae.
heptagon	a polygon with seven sides.
hexagon	a polygon with six sides.
hexahedron	a polyhedron with six faces. A regular hexahedron is a cube.
hypotenuse	the longest side of a right-angle triangle. The side opposite the right angle in a right triangle. 
irrational number	a number that is **not rational**. (*think: irresponsible means NOT responsible*). It cannot be calculated to perfect accuracy, it cannot be fully written down. It has **no** rational pattern of repetition in its decimal places. Examples of irrational numbers are π and $\sqrt{5}$, etc. It exists in your head but cannot be written down. Eg: $\sqrt{5}$ is the number than when two of them are multiplied together gives an answer of 5.

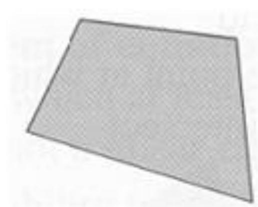
isosceles acute triangle:	a triangle with two equal sides and all angles less than 90° 
isosceles obtuse triangle:	a triangle with two equal sides and one angle greater than 90° 
isosceles right triangle:	a triangle with two equal sides and a 90° angle 
isosceles triangle:	a triangle with [at least] two equal sides
kite	a quadrilateral with two pairs of equal *adjacent* sides 

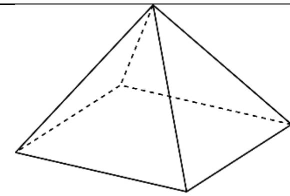
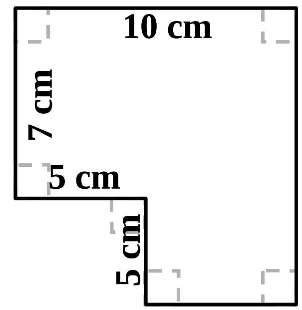
legs	the sides of a right triangle that form the right angle
parallelogram	a quadrilateral with both pairs of opposite sides parallel
octagon	a polygon with eight sides.  A 'regular' octagon has all sides and angles the same; congruent
octahedron	a polyhedron with eight faces.  We do lots of 3D shapes in Grade 11
parallel	describes two lines that are going the same direction and do not intersect.

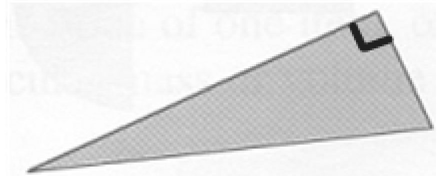
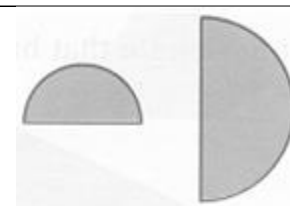
parallelogram	a quadrilateral with opposite sides parallel and consequently congruent in length. 
pentagon	a five sided polygon. 
perpendicular	two lines are perpendicular if the angle between them is 90 degrees. We use the math symbol: ‘ ⊥ ‘.
polygon	the union of three or more line segments that are joined together so as to completely enclose an area.
polyhedron	a solid 3-dimensional object that is bounded by plane polygons. We study polyhedrons like boxes and pyramids in Grade 11.
proportion	a statement that two ratios are equal. Eg: if one muffin takes 6 raisins, then 10 muffins takes 60 raisins. One boy for every six girls is the same as 10 boys for every 60 girls. $\frac{1}{6}=\frac{10}{60}$

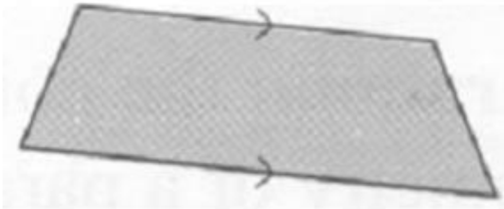
<table>
<tr><td>Pythagorean Theorem</td><td>for any right triangle, the area of the square on the hypotenuse is equal to the sum of the areas of the squares on the other two sides

or symbolically:
$\mathbf{c^2 = a^2 + b^2}$; provided that c is the hypotenuse length.</td><td>
</td></tr>
<tr><td>Pythagorean triple</td><td colspan="2">Three natural numbers that satisfy the Pythagorean theorem. One example is: 3, 4 and 5.

5, 12, 13 also works. So do an infinite number of other possibilities.</td></tr>
<tr><td>quadrilateral:</td><td colspan="2">a four-sided polygon
</td></tr>
<tr><td>rectangle</td><td colspan="2">a quadrilateral with four 90 degree [right] angles.</td></tr>
</table>

rectangular pyramid	a pyramid with a rectangular base 
rectilinear polygon	a shape made up of straight line segments where all the corners are 90° or square. 
regular polygon	a polygon in which all the angles have the same measure and all of the sides are equal in length.
repeating decimal	a decimal in which the decimal digits endlessly repeat a pattern. A repeating decimal can always be re-written as a fraction. Eg: **3.566566566566…** is **3563/999**
rhombus	a quadrilateral with four equal sides. Really just a square that is leaning. A rhombus is a special case of a parallelogram all sides the same length.
right angle	an angle whose measure is 90 degrees.

right triangle	a triangle that has a right angle. 
scale	the scale of an object is a comparison in a ratio or a fraction of its drawing or model size to its actual size. Scale → **Model : Actual** or $\frac{\textit{Model}}{\textit{Actual}}$ Many doll houses are **1:40** scale so **1 cm** (or unit) on the doll house is 40 cm (or units) on the real house. Boys' model airplanes are often **1/72** scale. A common scale for a city map is **1:100,000**, so that **1 cm** on the map is **1 km** in the actual city.
similar figures	figures with the same shape, but not necessarily the same size 
square of a number	To multiply two of the same number together. **3 * 3 = 9**; **6 * 6 = 36**; **25 * 25 = 625**. We often use a little 'two exponent' to write a square, eg: $\mathbf{6^2 = 36}$ or $\mathbf{9^2 = 81}$, etc. You have a button on your calculator that does a square, the $\mathbf{x^2}$ button.

square root	Square root of some number, **x**, is the desired number that, when multiplied by itself gives that number, **x**. for example, $\sqrt{9} = 3$because $\mathbf{3^2 = 9}$. To do a square root is really just to '*un-square*' a number. The $\sqrt{\ }$ is called the radical sign. The number inside it is called the radicand. In $\sqrt{10}$, 10 is called the *radicand*. Find that button on your calculator too. $\sqrt{\ }$
theorem	a statement that has been proven. A fact! A law.
trapezoid	a quadrilateral with one pair of opposite sides parallel but not equal in length.  [Fold it in half, then fold in the wings you have a rectangle!]
triangle	a three-sided polygon.

triangle types	Triangles have certain named characteristics depending on their lengths and also their angles. **Length Characteristic**: all three sides the same : equilateral at least two sides the same: Isosceles no two sides the same : scalene **Angle Characteristic**: all acute angles: acute triangle a 90 degree square corner: right triangle on obtuse angle (>90°): obtuse triangle