

Functions

Warmup

22-05-18

WARMUP 18 MAY

For the following quadratic function:

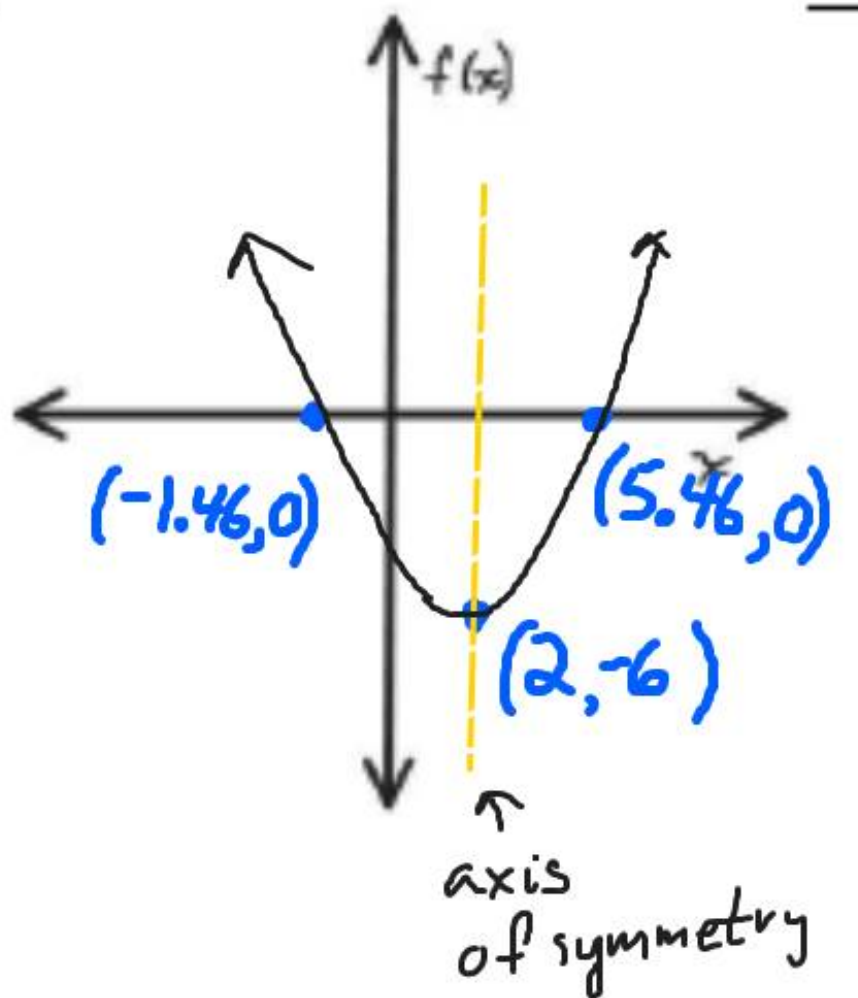
$$f(x) = \frac{1}{2}x^2 - 2x - 4$$

a. Make a representative sketch of the function. Significant points should be in correct quadrants.

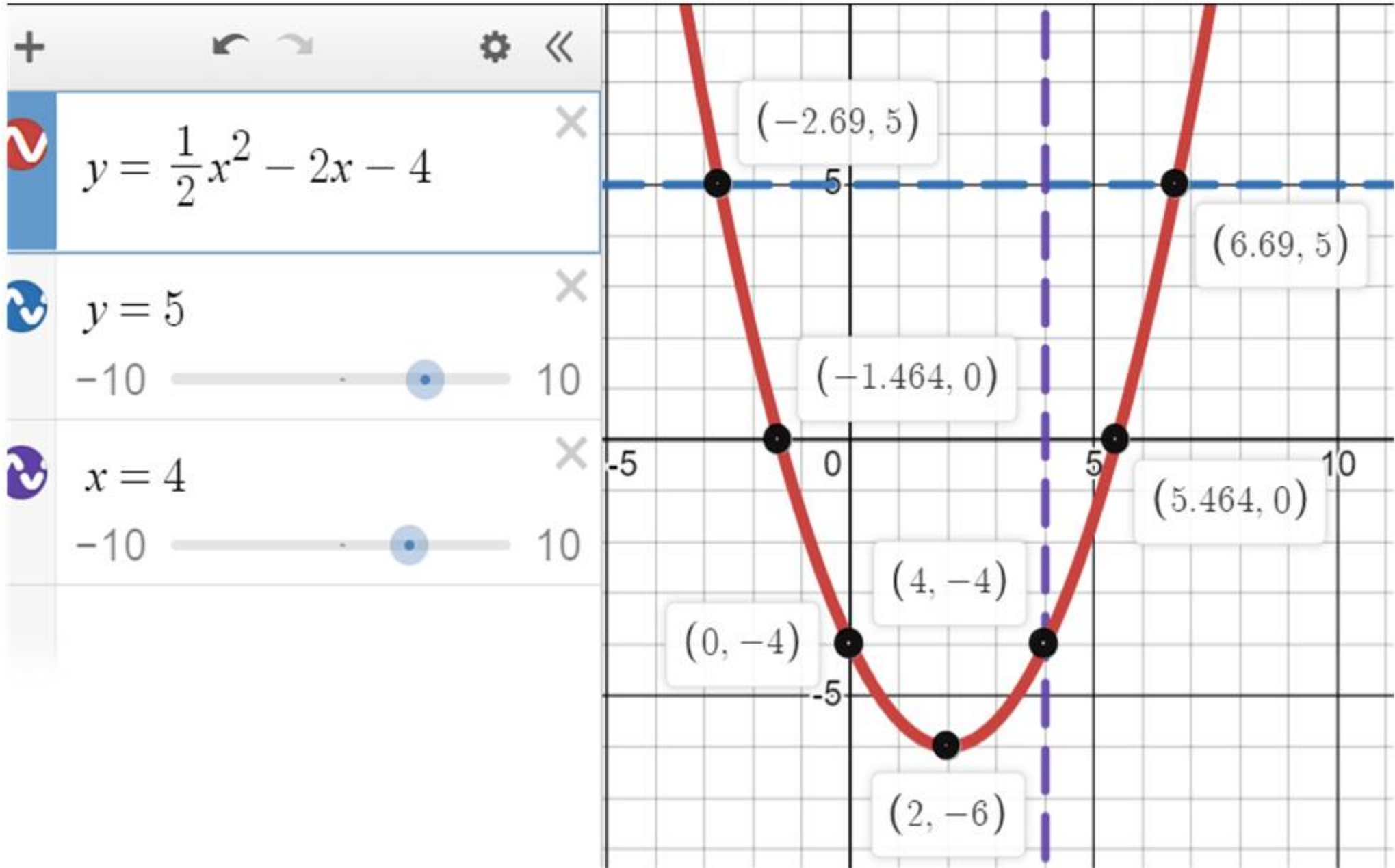
b. State the Domain and the Range

$$\{ -\infty < x < +\infty \}$$

$$\{ -6 \leq f(x) < +\infty \}$$



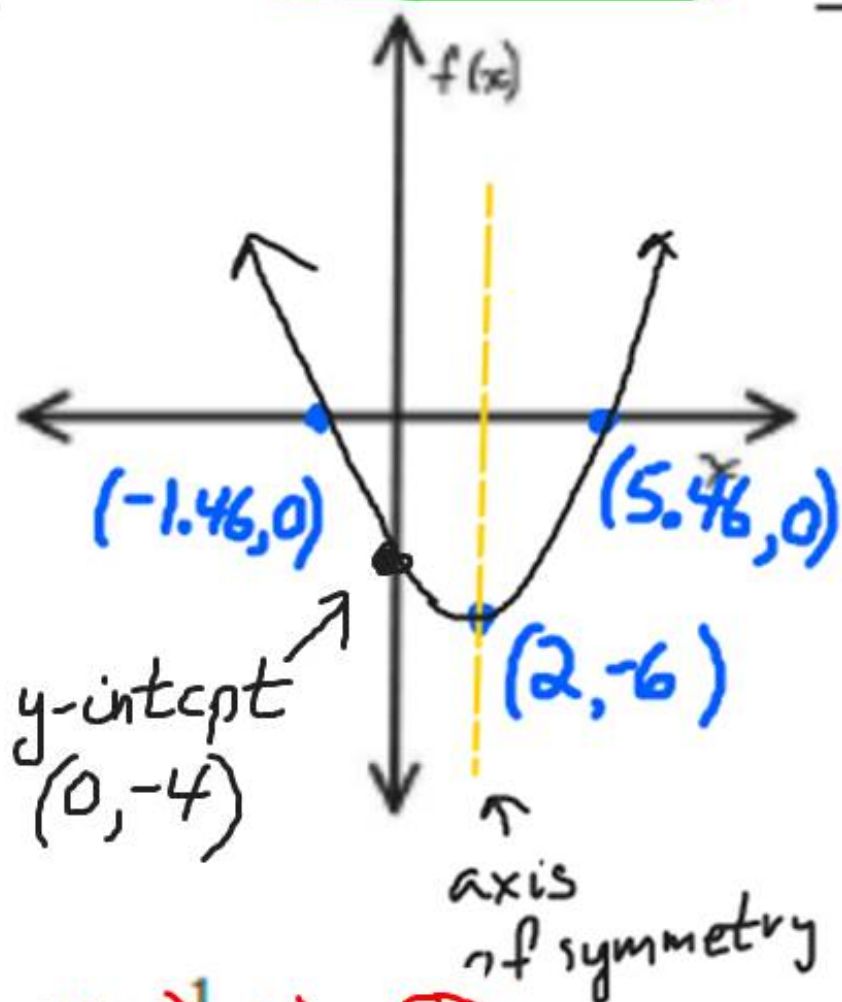
Takes 1 min to figure out the answers!



c. Indicate on the sketch and state the following.

Vertex: $(\underline{2}, \underline{-6})$

Axis of Symmetry: $x = \underline{2}$



$$f(0) = \frac{1}{2} \cdot 0^2 - 2 \cdot 0 - 4$$

d. Indicate on the sketch and state:

y - intercept: $(\underline{0}, \underline{-4})$

'zeros' [x - intercept(s)] if any

$(\underline{-1.46}, \underline{0}) ; (\underline{5.46}, \underline{0})$

e. State the minimum value of the function: _____

-6 is the min value from vertex

f. solve for x:

$$5 = \frac{1}{2}x^2 - 2x - 4$$

x = $\{ \underline{-2.69}, \underline{+6.69} \}$

it works!

$$\frac{1}{2} \cdot (6.69)^2 - 2 \cdot (6.69) - 4 = 4.99805$$

g. evaluate: $f(4) = \underline{-4}$

$$\begin{aligned} f(4) &= \frac{1}{2}(4)^2 - 2(4) - 4 \\ &= 8 - 8 - 4 = \underline{-4} \end{aligned}$$

For the following exponential function:

$$f(x) = 100 * 2^x$$

a. Make a representative sketch of the function. Significant points should be in correct quadrants.

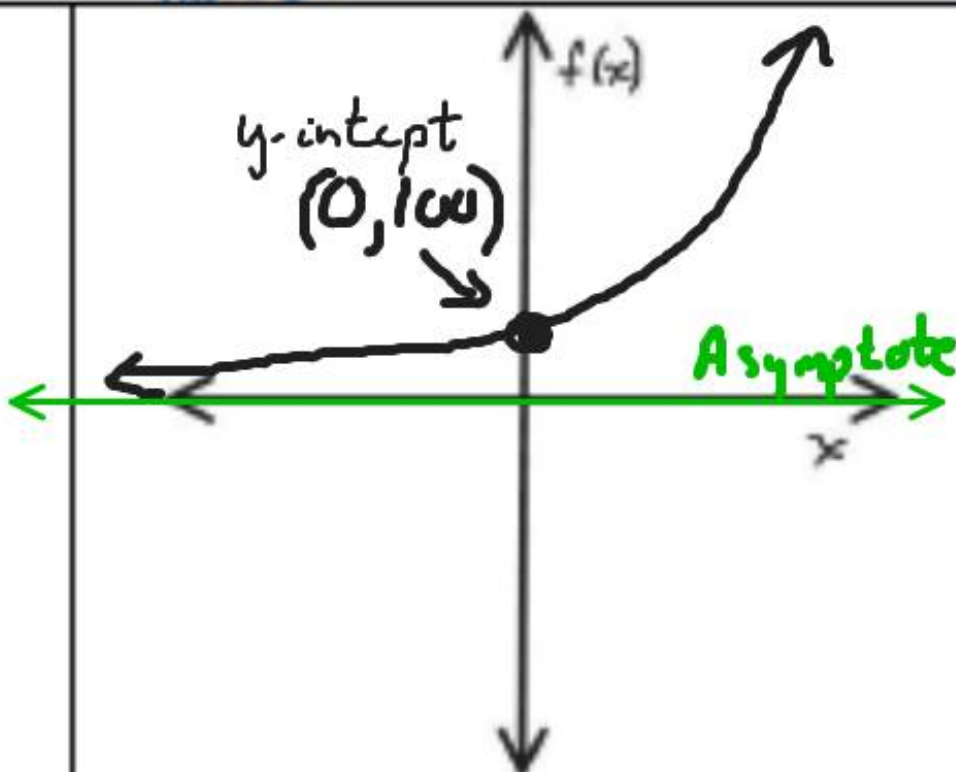
b. State the Domain and the Range

$$\{ -\infty < x < +\infty \}$$

$$\{ 0 < f(x) < \infty \}$$

c. Indicate on the sketch and state the following.

Asymptote: $y = 0$
Approaches 0 at $-\infty$
~~Axis of Symmetry: $x =$ _____~~



d. Indicate on the sketch and state:

y - intercept: $(0, 100)$

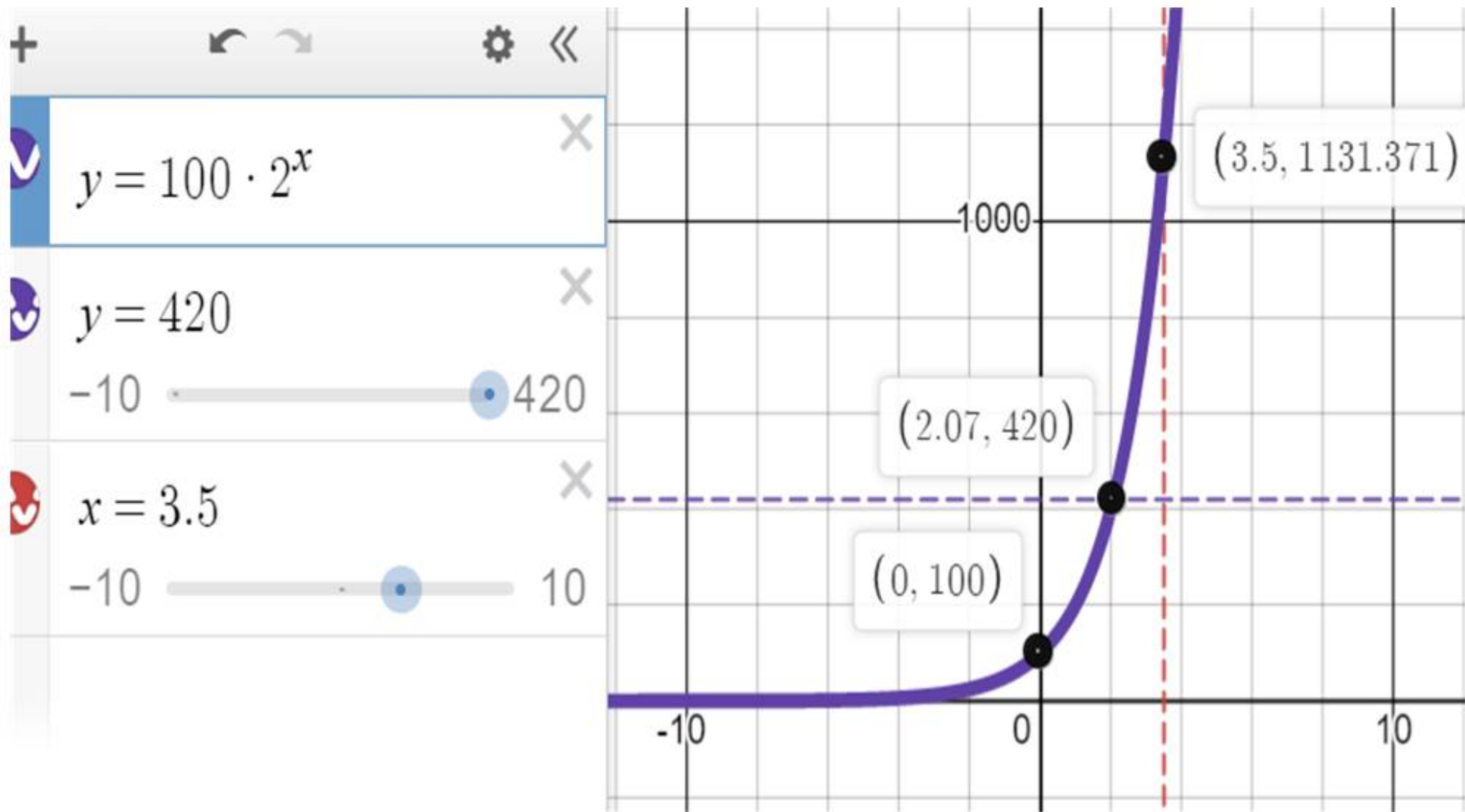
'zeros' [x - intercept(s)] if any

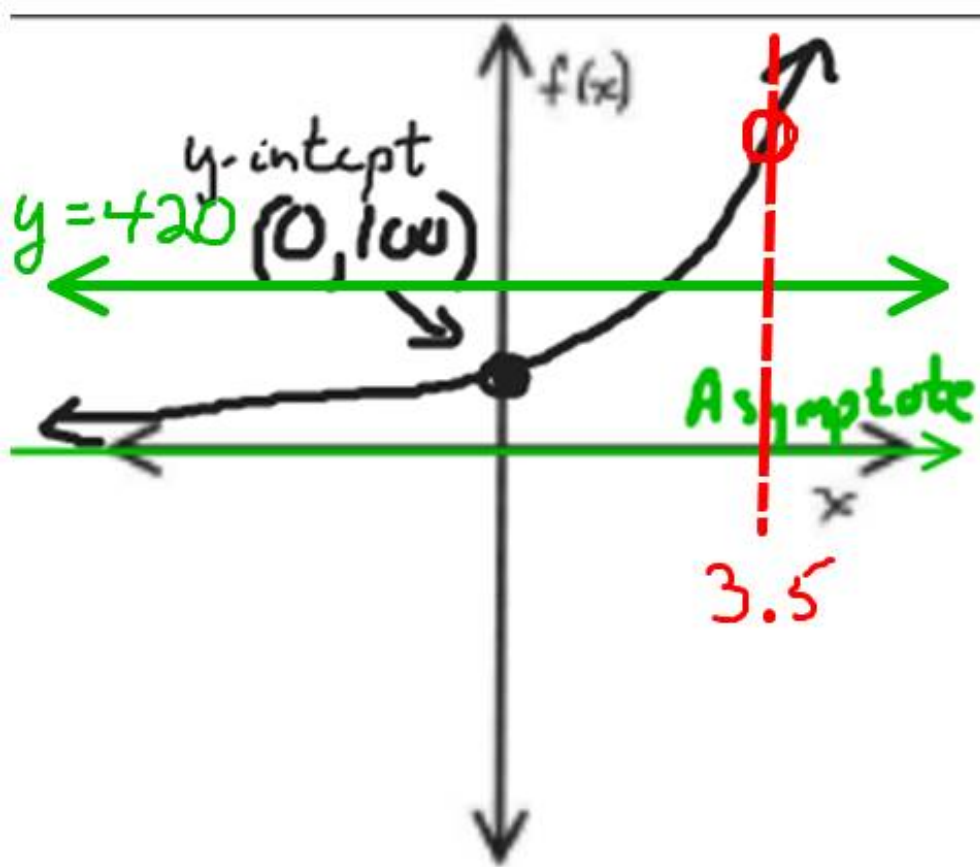
$(\text{---}, \text{---})$, $(\text{---}, \text{---})$
Nil

There are none

Can you do some of this in your head?

Easy Peasy





e. state the minimum or maximum value of the function:

The minimum "approaches" zero asymptotically

f. solve for x:

$$420 = 100 + 2^x$$

$$x = \underline{2.07}$$

$$100 * 2^{2.07} \checkmark$$

$$419.8861$$

checks

g. Evaluate: $f(3.5) = \underline{1131.37}$

$$f(3.5) = 100 \cdot 2^{3.5}$$

$$= 1131.37$$

3 doublings would be 800
 3.5 doublings \rightarrow 1131
 4 doublings would be 1600
 Sounds about right