

GRADE 12 APPLIED
UNIT B – PERSONAL FINANCE
LOANS

Name: _____

Date: _____

Recall Grade 11 Essential Interest and Credit Studies.

We had used **tables** to determine the regular monthly loan payments to pay off a loan (fixed rate) over some amortization period. The tables were provided in your notes and printed as separate coloured table.

You have learned about Simple and Compound interest on an investment or a loan in which you invest or borrow a fixed sum of money (present Value, PV) for a certain time and the re-payment (Future Value, FV) occurs all in one shot.

For example, you borrow \$2,000 from your uncle and he gets \$3,000 back in one single payment after two years. In reality though, very few banks are willing to loan you money and say: “come back in a couple years and pay us back”. They want monthly installments to make sure you are still in town! Further, paying off the loan (amortizing the loan) in installments makes it cheaper for you too because you start paying it off right away and you don’t end up with a big ‘surprise’ at the end of the loan period for a lot of money to pay back. There is a huge unwieldy formula you can use to calculate your loan payments and loads of apps and websites that readily do the calculation.

$$P = \frac{r * M}{1 - \left(1 + \frac{r}{n}\right)^{-nt}} \div n$$

where ‘P’ is the monthly payment, ; ‘r’ the annual interest rate;

‘M’ the mortgage amount; ‘t’ the number of years to ‘amortize’; and ‘n’ is the number of payments per year. So a computer or an App is preferred!

The loan tables we used were a simple way to calculate a monthly loan payment.

2. You borrow \$6,500 from the bank at 9% interest (compounded monthly) and want to pay it off (amortize it, 'mort' in French means kill) after 5 years. Using tables answer the following:

- what will your monthly payments be?
- how many monthly payments do you make pay off the loan?
- how much will you have paid at the end of the loan total?
- what was your cost to borrow that money (ie: the interest you paid)

3. Now do it on a TVM App

N=
I%=
PV=
PMT=
FV=
P/Y=
C/Y=
PMT:  BEGIN

Remember **N** = the number of periods.

PMT is the Payment amount we will solve for

P/Y [Payments per year] and C/Y [Compoundings per year] are 12

You start making your first payment at the END of the first month and subsequent months thereafter.

4. The TVM App allows us to get considerably more fancy!

5. Would you believe that if you made your regular loan payments every two weeks ('bi-weekly') on pay day, that you would end up paying less for the loan in the end!

Try it. →

Hint: there are 26 bi-weekly periods in a year

Mode End Beginning

| | | |
|-----------------|--|--|
| Present Value | <input type="text"/> | <input type="button" value="PV"/> |
| Payments | <input type="text"/> | <input type="button" value="PMT"/> |
| Future Value | <input type="text"/> | <input type="button" value="FV"/> |
| Annual Rate (%) | <input type="text"/> | <input type="button" value="Rate"/> |
| Periods | <input type="text"/> | <input type="button" value="Periods"/> |
| Compounding | <input type="text" value="Bi-Weekly"/> | |

6. If you paid bi-weekly how did that compare with the monthly loan payment calculation? Complete the table:

| | Periodic Payment | Total Amount Paid | Cost of Loan (Interest) |
|-----------|------------------|-------------------|-------------------------|
| Monthly | | | |
| Bi-Weekly | | | |

7. You borrow \$250,000 from the bank for a house loan (ie: mortgage) at 8.5% interest and want to pay it off after 10 years. Use the manual method with tables again. (*need to interpolate the table value, halfway between 8% and 9%*)

- what will your **monthly** payments be?
- how many monthly payments do you make pay off the loan?
- how much will you have paid at the end of the loan total?
- what was your cost to borrow that money (ie: the interest you paid)?
- how much would the loan have cost you in interest if you had paid it off in 5 years instead? (Need to look it up in tables again!)

8. Calculate it again on a TVM App to find the **monthly** payments.

Why do you not get exactly the same answer as the table method??

```

N=
I%=
PV=
PMT=
FV=
P/Y=
C/Y=
PMT:  END  BEGIN

```



9. Calculate it with bi-weekly payments. Assume the Compounding interval is still monthly

So in effect you are making 13 payments a year instead of 12. Paying it down quicker

Mode End Beginning

Present Value

Payments

Future Value

Annual Rate (%)

Periods

Compounding

10. If you paid off your \$250,000 mortgage bi-weekly how did that compare with the monthly loan payment calculation? Do the calculations. Complete the table:

| | Periodic Payment | Total Amount Paid | Cost of Loan (Interest) |
|-----------|------------------|-------------------|-------------------------|
| Monthly | | | |
| Bi-Weekly | | | |

Solving for other arguments (variables) in the Loan Equation

11. You know you can afford \$1,200/month mortgage payments. Present mortgage rates are 3.75% compounded the end of every month. You will take a fixed rate mortgage of that 3.75% for 25 years. So how much of a house mortgage can you afford if you pay monthly.

Caution: There are of course there are other monthly costs to affording a house, heat and property taxes being biggies; perhaps another \$350 - \$450 per month. Maybe also maintenance, home insurance [\$700 / year], etc.

N=
 I%=
 PV=
 PMT=
 FV=
 P/Y=
 C/Y=
 PMT: END BEGIN

End Beginning

MrF

12. As per the previous question how much house could you afford if you decide to work lots of over time; be a hermit, no smoking, no parties, no bingo; and pay off the house in 10 years. You will make monthly payments of \$3,000.

N=
I%=
PV=
PMT=
FV=
P/Y=
C/Y=
PMT: END BEGIN

13. Your partner has their eye on the perfect house for your family. A great neighbourhood, school down the block, it is only \$285K. Of course, you will need to make a down payment of 10% of that up-front. So, you will need to finance at the bank for a mortgage of \$256.5K (256,500). You can afford \$1,700 / month for the mortgage payments.

14. Determine what interest rate you will need acquire / negotiate for 25 years to afford the mortgage.

You need an interest rate of _____ or better.

N=
I%=
PV=
PMT=
FV=
P/Y=
C/Y=
PMT: END BEGIN

15. How does a bank determine initially if you can afford a mortgage?

They calculate a **Gross Debt Service Ratio**. They want to make sure you can afford the house and not be spending more than 32% of your Gross Income on your house.

$$\text{Gross Debt Service ratio (\%)} = \frac{\left(\begin{array}{ccc} \text{Monthly} & \text{Monthly} & \text{Monthly} \\ \text{Mortgage} & + \text{Property} & + \text{Heating} \\ \text{Payment} & \text{Taxes} & \text{Costs} \end{array} \right)}{\text{Gross Monthly Income}} * 100; \text{ max } 32\%$$

16. Mr. and Mrs. Spence have a total monthly gross income of \$6,000.00. They are interested in purchasing a house with a mortgage payment of \$1,300.00 per month, annual heating costs of \$2,100.00, and annual property taxes (including school taxes) of \$3,675.00.

- a. Calculate the gross debt service ratio (GDSR).
- b. Determine if a bank is likely to offer them a mortgage.

17. Marshall and Kim are renting a house that they hope to purchase. They pay \$1,800 in annual heating costs and know that the annual property taxes are \$2,500. Their combined gross income is \$5,200 per month.

- a) Based on the gross debt service ratio (GDSR), what is the maximum monthly mortgage payment they can afford?
- b) If they have saved \$30,000.00 for a down payment, what is the maximum house price they can afford based on a 25-year amortization period at an interest rate of 4.64%, compounded semi-annually?