

# 11-7 Trigonometric Ratios (Pages 623–630)

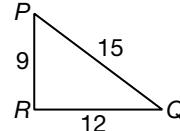
In a right triangle, the side opposite the right angle is the longest side. This side is called the **hypotenuse**. The other two sides are the **legs**.

<b>Definition of Trigonometric Ratios</b>	sine of $\angle A = \frac{\text{measure of leg opposite } \angle A}{\text{measure of hypotenuse}}$ cosine of $\angle A = \frac{\text{measure of leg adjacent } \angle A}{\text{measure of hypotenuse}}$ tangent of $\angle A = \frac{\text{measure of leg opposite } \angle A}{\text{measure of leg adjacent } \angle A}$	$\sin A = \frac{a}{c}$ $\cos A = \frac{b}{c}$ $\tan A = \frac{a}{b}$	

### Examples

- a. Find the sine, cosine, and tangent of angle Q.

$$\begin{aligned} \sin Q &= \frac{\text{opposite leg}}{\text{hypotenuse}} & \cos Q &= \frac{\text{adjacent leg}}{\text{hypotenuse}} & \tan Q &= \frac{\text{opposite leg}}{\text{adjacent leg}} \\ &= \frac{9}{15} \text{ or } 0.6 & &= \frac{12}{15} \text{ or } 0.8 & &= \frac{9}{12} \text{ or } 0.75 \end{aligned}$$



- b. Find the measure of angle P,  $m\angle P$ , to the nearest degree.

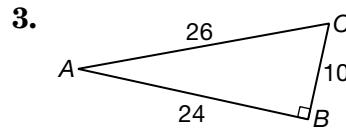
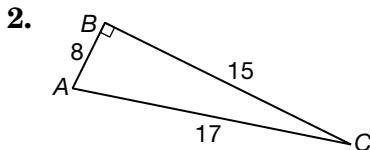
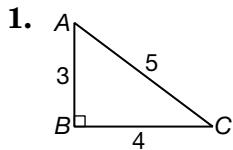
$$\sin P = \frac{\text{opposite leg}}{\text{hypotenuse}} \Rightarrow \sin P = \frac{12}{15} \text{ or } 0.8$$

Use a scientific calculator to find the angle measure with a sine of 0.8.

Enter: 0.8 [2nd] [SIN<sup>-1</sup>] Result: 53.13010235 So,  $m\angle P \approx 53^\circ$ .

### Practice

For each triangle, find  $\sin C$ ,  $\cos C$ , and  $\tan C$  to the nearest thousandth. Use a calculator to find the value of each trigonometric ratio to the nearest ten thousandth if necessary.



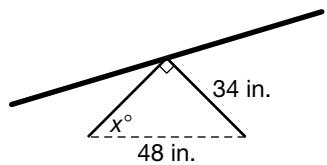
1.  $\sin 14^\circ$     5.  $\cos 68^\circ$     6.  $\tan 80^\circ$     7.  $\cos 60^\circ$     8.  $\sin 85^\circ$

Use a calculator to find the measure of each angle to the nearest degree.

9.  $\sin B = 0.8192$     10.  $\cos M = 0.7660$     11.  $\tan W = 0.2309$   
 12.  $\cos Y = 0.7071$     13.  $\sin P = 0.9052$     14.  $\tan K = 0.2675$

15. **Standardized Test Practice** Which equation can be used to find the measure of the angle measuring  $x^\circ$  under the seesaw?

- A  $\sin(x^\circ) = \frac{48}{34}$     B  $\cos(x^\circ) = \frac{48}{34}$   
 C  $\sin(x^\circ) = \frac{34}{48}$     D  $\tan(x^\circ) = \frac{34}{48}$



4. 0.2419	5. 0.3746	6. 0.56713	7. 0.5	8. 0.9962	9. 55°	10. 40°	11. 13°	12. 45°	13. 65°	14. 15°	15. C
<b>Answers:</b> 1. $\sin C = \frac{3}{5}$ ; $\cos C = \frac{4}{5}$ ; $\tan C = \frac{3}{4}$ 2. $\sin C = \frac{3}{4}$ ; $\cos C = \frac{8}{17}$ ; $\tan C = \frac{15}{8}$ 3. $\sin C = \frac{12}{13}$ ; $\cos C = \frac{5}{13}$ ; $\tan C = \frac{12}{5}$											