Grade 10 Essential Mathematics

UNIT X – REVIEW / PRIOR STUDIES FRACTIONS

This is a review of fractions from prior grades

Multiplication Lesson 1

Multiply the numerators.

$$\frac{1}{2} \times \frac{3}{5} \times \frac{3}{4} = \frac{1 \times 3 \times 3}{2 \times 5 \times 4} = \frac{9}{40}$$

Multiply the denominators.

$$\frac{1}{2} \times \frac{3}{4} = \frac{1 \times 3}{2 \times 4} = \frac{3}{8}$$

$$\frac{4}{5} \times \frac{2}{3} \times \frac{1}{3} = \frac{4 \times 2 \times 1}{5 \times 3 \times 3} = \frac{8}{45}$$

Multiply.

$$\boldsymbol{a}$$

1.
$$\frac{3}{4} \times \frac{1}{5}$$

$$\frac{2}{3} \times \frac{2}{5}$$

$$\frac{7}{8} \times \frac{5}{6} \times \frac{1}{2}$$

$$\frac{3}{4} \times \frac{1}{5}$$
 $\frac{2}{3} \times \frac{4}{5}$ $\frac{7}{8} \times \frac{5}{6} \times \frac{1}{2}$ $\frac{3}{5} \times \frac{2}{7} \times \frac{1}{5}$

$$2. \qquad \frac{1}{2} \times \frac{1}{3}$$

$$\frac{4}{5} \times \frac{2}{7}$$

$$\frac{3}{8} \times \frac{3}{5} \times \frac{3}{4}$$

$$\frac{1}{2} \times \frac{1}{4} \times \frac{1}{3}$$

3.
$$\frac{5}{8} \times \frac{5}{8}$$

$$\frac{6}{7} \times \frac{3}{5}$$

$$\frac{2}{3} \times \frac{1}{5} \times \frac{1}{7}$$

$$\frac{3}{7} \times \frac{1}{5} \times \frac{3}{4}$$

4.
$$\frac{3}{8} \times \frac{5}{7}$$

$$\frac{5}{7} \times \frac{3}{8}$$

$$\frac{4}{5} \times \frac{4}{5} \times \frac{4}{5}$$

$$\frac{2}{3} \times \frac{2}{3} \times \frac{2}{3}$$

5.
$$\frac{3}{5} \times \frac{2}{5}$$

$$\frac{7}{8} \times \frac{3}{10}$$

$$\frac{5}{6} \times \frac{5}{9} \times \frac{1}{2}$$

$$\frac{3}{5} \times \frac{2}{5} \times \frac{4}{5}$$

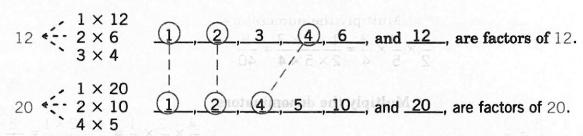
6.
$$\frac{3}{5} \times \frac{1}{2}$$

$$\frac{5}{8} \times \frac{7}{9}$$

$$\frac{3}{8} \times \frac{5}{7} \times \frac{3}{4}$$

$$\frac{2}{3} \times \frac{4}{5} \times \frac{1}{7}$$

Lesson 2 Greatest Common Factor



1, 2, and 4 are **common factors** of 12 and 20. 4 is the **greatest common factor** of 12 and 20.

List the factors of each number named below. Then list the common factors and the greatest common factor of each pair of numbers.

| | factors | common | factor(s) | greatest common factor |
|------------------------|---------------|---|--|--------------------------------|
| 1. | 6 | <u> </u> | ÷×, | <u> </u> |
| -9 | 10 | 3 5 7 - | \$ X 7 | |
| 4. | 16 24 9 | 4 4 4 | $\frac{\tilde{c}}{8} \times \frac{\tilde{c}}{7}$ | \$ × \frac{2}{5} × \frac{2}{5} |
| 5. | 16 | $\frac{5}{6} \times \frac{5}{9} \times \frac{1}{2}$ | 8 TO | <u> </u> |
| | 2524 | $\frac{3}{8} \times \frac{5}{7} \times \frac{3}{4} = \frac{3}{4}$ | \$\frac{5}{8} \times \frac{8}{9} | |
| 7. | 36 | | | |

Lesson 3 Simplest Form

A fraction is in simplest form when the greatest common factor of the numerator and denominator is 1.

Divide 8 and 12 by their greatest common factor.

$$\frac{8}{12} = \frac{8 \div 4}{12 \div 4} = \frac{2}{3}$$

The simplest form for $\frac{8}{12}$ is $\frac{2}{3}$.

A mixed numeral is in simplest form when its fraction is in simplest form and names a number between 0 and 1.

Divide 10 and 15 by their greatest common factor.

$$8\frac{10}{15} = 8\frac{10 \div 5}{15 \div 5} = 8\frac{2}{3}$$

CHAPTER 2

The simplest form for $8\frac{10}{15}$ is _____.

Write each of the following in simplest form.

1.
$$\frac{6}{15}$$

$$\frac{12}{20}$$

$$\frac{21}{30}$$

2.
$$\frac{16}{36}$$

$$\frac{40}{42}$$

$$\frac{18}{36}$$

3.
$$2\frac{9}{15}$$

$$6\frac{18}{30}$$

$$8\frac{36}{54}$$

4.
$$\frac{10}{35}$$

$$3\frac{4}{18}$$

$$7\frac{18}{24}$$

5.
$$5\frac{18}{45}$$

Lesson 4 Simplifying Products

Study the two ways $\frac{6}{7} \times \frac{3}{4}$ is found in simplest form.

$$\frac{6}{7} \times \frac{3}{4} = \frac{6 \times 3}{7 \times 4}$$

$$= \frac{18}{28}$$

$$= \frac{18 \div 2}{28 \div 2}$$

$$= \frac{3}{7}$$

$$= \frac{3}{7}$$

$$\frac{6}{7} \times \frac{3}{4} = \frac{\cancel{6} \times \cancel{3}}{\cancel{7} \times \cancel{4}}$$

$$= \frac{3 \times 3}{\cancel{7} \times \cancel{4}}$$

 $\frac{6}{7} \times \frac{3}{4} = \frac{6 \times 3}{7 \times 4}$ Divide 6 (in the numerator) and -4 (in the denominator) by their greatest common factor, 2.

1.
$$\frac{4}{5} \times \frac{1}{2}$$

$$\frac{b}{8} \times \frac{2}{3}$$

$$\frac{c}{5} \times \frac{4}{9}$$

$$\frac{a}{9} \times \frac{7}{10}$$

2.
$$\frac{2}{3} \times \frac{5}{6}$$

$$\frac{7}{10} \times \frac{8}{9}$$

$$\frac{10}{11} \times \frac{7}{12}$$

$$\frac{5}{7} \times \frac{3}{10}$$

3.
$$\frac{7}{9} \times \frac{6}{11}$$

$$\frac{12}{13} \times \frac{3}{4}$$

$$\frac{10}{11} \times \frac{7}{15}$$

$$\frac{8}{9} \times \frac{5}{12}$$

4.
$$\frac{5}{8} \times \frac{2}{5}$$

$$\frac{9}{16} \times \frac{1}{6}$$

$$\frac{1}{2} \times \frac{8}{9}$$

$$\frac{4}{7} \times \frac{14}{15}$$

5.
$$\frac{3}{8} \times \frac{4}{5}$$

$$\frac{8}{9} \times \frac{6}{7}$$

$$\frac{4}{7} \times \frac{5}{6}$$

$$\frac{4}{15} \times \frac{12}{13}$$

Lesson 4 Simplifying Products

Study the two ways $\frac{6}{7} \times \frac{3}{4}$ is found in simplest form.

$$\frac{6}{7} \times \frac{3}{4} = \frac{6 \times 3}{7 \times 4}$$

$$= \frac{18}{28}$$

$$= \frac{18 \div 2}{28 \div 2}$$

$$= \frac{3}{7}$$

$$\frac{6}{7} \times \frac{3}{4} = \frac{\cancel{6} \times \cancel{3}}{\cancel{7} \times \cancel{4}}$$

$$= \frac{3 \times \cancel{3}}{\cancel{7} \times \cancel{2}}$$

Divide 6 (in the numerator) and — 4 (in the denominator) by their greatest common factor, 2.

1.
$$\frac{4}{5} \times \frac{1}{2}$$

$$\frac{3}{8} \times \frac{2}{3}$$

$$\frac{c}{5} \times \frac{4}{9}$$

$$\frac{a}{9} \times \frac{7}{10}$$

2.
$$\frac{2}{3} \times \frac{5}{6}$$

$$\frac{7}{10} \times \frac{8}{9}$$

$$\frac{10}{11} \times \frac{7}{12}$$

$$\frac{5}{7} \times \frac{3}{10}$$

3.
$$\frac{7}{9} \times \frac{6}{11}$$

$$\frac{12}{13} \times \frac{3}{4}$$

$$\frac{10}{11} \times \frac{7}{15}$$

$$\frac{8}{9} \times \frac{5}{12}$$

4.
$$\frac{5}{8} \times \frac{2}{5}$$

$$\frac{9}{16} \times \frac{1}{6}$$

$$\frac{1}{2} \times \frac{8}{9}$$

$$\frac{4}{7} \times \frac{14}{15}$$

5.
$$\frac{3}{8} \times \frac{4}{5}$$

$$\frac{8}{9} \times \frac{6}{7}$$

$$\frac{4}{7} \times \frac{5}{6}$$

$$\frac{4}{15} \times \frac{12}{13}$$

Lesson 5 Simplifying Products

Study how $\frac{5}{6} \times \frac{9}{10} \times \frac{1}{7}$ is found in simplest form.

$$\frac{\cancel{5} \times 9 \times 1}{6 \times \cancel{10} \times 7}$$

Both numerator and denominator have been divided by _____.

$$\frac{\cancel{5} \times \cancel{9} \times 1}{\cancel{5} \times \cancel{10} \times 7}$$

Both numerator and denominator have been divided by ____.

$$\frac{\cancel{\cancel{5}} \times \cancel{\cancel{5}} \times \cancel{1}}{\cancel{\cancel{5}} \times \cancel{\cancel{10}} \times \cancel{7}} = \frac{1 \times 3 \times 1}{2 \times 2 \times 7}$$

 $=\frac{3}{28}$

$$\frac{5}{6} \times \frac{9}{10} \times \frac{1}{7} = \underline{\hspace{1cm}}$$

Write each answer in simplest form.

(

1.
$$\frac{3}{5} \times \frac{5}{6}$$

b

$$\frac{4}{9} \times \frac{3}{8}$$

c

$$\frac{7}{8} \times \frac{6}{7}$$

a

$$\frac{2}{3} \times \frac{3}{4} \times \frac{1}{5}$$

2.
$$\frac{9}{10} \times \frac{5}{6}$$

$$\frac{5}{8} \times \frac{4}{15}$$

$$\frac{10}{11} \times \frac{11}{12}$$

$$\frac{4}{5} \times \frac{3}{4} \times \frac{5}{6}$$

3.
$$\frac{7}{9} \times \frac{9}{14}$$

$$\frac{4}{5} \times \frac{5}{12}$$

$$\frac{3}{4} \times \frac{8}{9}$$

$$\frac{4}{7} \times \frac{2}{3} \times \frac{7}{8}$$

4.
$$\frac{4}{9} \times \frac{9}{10}$$

$$\frac{2}{3} \times \frac{9}{10}$$

$$\frac{3}{10} \times \frac{5}{6}$$

$$\frac{2}{5} \times \frac{3}{4} \times \frac{5}{6}$$

5.
$$\frac{5}{9} \times \frac{9}{10}$$

$$\frac{7}{8} \times \frac{2}{7}$$

$$\frac{3}{10} \times \frac{5}{9}$$

$$\frac{4}{7} \times \frac{7}{8} \times \frac{2}{3}$$

Lesson 6 Renaming Fractions and Mixed Numerals

An improper fraction has its numerator greater than its denominator.

Change $3\frac{2}{5}$ to an improper fraction.

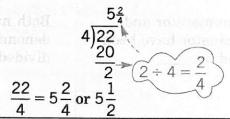
$$3\frac{2}{5} = \frac{(5 \times 3) + 2}{5}$$

$$= \frac{15 + 2}{5}$$

$$= \frac{17}{5}$$

Change $\frac{22}{4}$ to a mixed numeral.

 $\frac{22}{4}$ means 22 ÷ 4 or 4)22.



You can think of every whole number as an improper fraction with a denominator of 1.

$$2 = \frac{2}{1}$$

$$5 = \frac{5}{1}$$

$$21 = \frac{21}{1}$$

Change each of the following to an improper fraction.

1.
$$1\frac{7}{10}$$

$$\boldsymbol{c}$$

2.
$$2\frac{3}{4}$$

$$3\frac{5}{6}$$

$$5\frac{1}{3}$$

$$6\frac{7}{8}$$

Change each of the following to a mixed numeral in simplest form.

3.
$$\frac{9}{4}$$

$$\frac{21}{5}$$

$$\frac{9}{6}$$

$$\frac{18}{8}$$

$$2\frac{9}{5}$$

4.
$$\frac{43}{8}$$

$$\frac{64}{10}$$

$$\frac{22}{4}$$

$$\frac{16}{12}$$

$$5\frac{15}{10}$$

5.
$$\frac{22}{3}$$

$$\frac{36}{7}$$

$$\frac{15}{6}$$

$$\frac{27}{4}$$

$$\frac{41}{8}$$

Lesson 7 Multiplication (mixed numerals)

$$6 \times 5\frac{3}{4} = \frac{6}{1} \times \frac{23}{4}$$
$$= \frac{\cancel{6} \times 23}{\cancel{1} \times \cancel{4}}$$
$$= \frac{69}{\cancel{1}}$$

 $=34\frac{1}{2}$

Rename the numbers as improper fractions.

$$2\frac{2}{3} \times 1\frac{1}{2} \times \frac{4}{5} = \frac{8}{3} \times \frac{3}{2} \times \frac{4}{5}$$

$$- \cancel{8} \times \cancel{3} \times 4$$

Divide the numerator and the $= \frac{\cancel{8} \times \cancel{3} \times \cancel{4}}{\cancel{3} \times \cancel{2} \times 5}$ denominator by common factors. To abrid towT stun to easy to but = $\frac{4 \times 1 \times 4}{1 \times 1 \times 5}$ $=\frac{69}{2}$ Multiply. Write the product as a mixed

 $=\frac{16}{5}$ or $3\frac{1}{5}$

Write each answer in simplest form.

numeral in simplest form.

1.
$$8 \times 2\frac{5}{6}$$

$$4\frac{2}{3}\times9$$

$$3\frac{1}{6} \times 2 \times 9$$

2.
$$1\frac{2}{3} \times 1\frac{1}{5}$$

$$1\frac{2}{7} \times 2\frac{1}{3}$$

$$1\frac{1}{3} \times 1\frac{1}{8} \times 1\frac{2}{3}$$

3.
$$1\frac{1}{9} \times \frac{3}{8}$$

$$\frac{5}{6} \times 1\frac{1}{8}$$

$$\frac{5}{6} \times 1\frac{1}{8} \qquad \qquad \frac{4}{5} \times 3\frac{1}{2} \times 2\frac{1}{2}$$

4.
$$3\frac{1}{3} \times 1\frac{1}{5}$$

$$2\frac{2}{5} \times \frac{5}{8}$$

$$2\frac{1}{3} \times \frac{3}{7} \times \frac{1}{2}$$

5.
$$1\frac{2}{3} \times 2\frac{2}{5}$$

$$\frac{1}{6} \times 3\frac{1}{3}$$

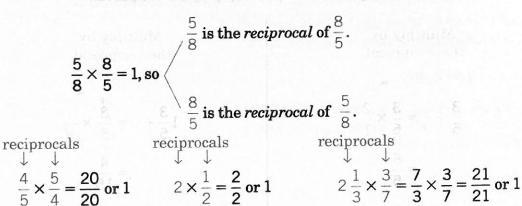
$$1\frac{1}{4} \times \frac{2}{3} \times 2\frac{1}{2}$$

Lesson 7 Problem Solving

| | 그는 사람들이 하나 바람이 가지 하는 이 아이들이 있다면 살아 하는 것 같아. 그는 사람들이 아니는 | | |
|----|---|---------------|-----------------------|
| 1. | Ava has $1\frac{1}{2}$ sacks of flour. Each sack has a mass of 6 kg. How many kilograms of flour does Ava have? | 1. Enderburt | |
| | Ava has kg of flour. | de caraela | |
| 2. | Mr. DiMaggio had $1\frac{3}{4}$ bags of nuts. Two thirds of this amount was used at a dinner party. How many bags of nuts were used? | Write the p | <u>ea</u> S = 1 |
| | bags of nuts were used. | | |
| 3. | Alyson is writing an essay. She wrote $2\frac{3}{4}$ pages in the first hour. At that rate, how many pages will she write in $3\frac{3}{5}h$? | 3.1 resignate | d rezeba done a sez |
| | She will write pages. | 4 8 | |
| 4. | In problem 3, how many pages will she write in 8 h? | 4. | |
| | She will write pages. | | |
| 5. | Louis has 16 rookie hockey cards. Anne has $2\frac{1}{4}$ times that many rookie cards. How many rookie cards does Anne have? | 5. | |
| | Anne has rookie cards. | | |
| 6. | In a relay, each person runs $5\frac{5}{6}$ laps around a track. There are 16 people on the relay team. How many laps are run in all? | 6. | |
| | laps are run in all. | | |
| 7. | $7\frac{2}{3}$ small oranges have a mass of 1 kg. How many oranges would have a mass of 36 kg? | 7. | |
| | small oranges would have a mass of 36 kg. | | |
| | Alex has $3\frac{4}{5}$ full albums of stamps. John has $3\frac{2}{3}$ times as many full albums of stamps. How many albums of stamps does John have? | 8. | |
| | John has albums of stamps. | | |

Lesson 8 Reciprocals

If the product of two numbers is 1, the numbers are reciprocals of each other.



Tell whether the fractions in each pair are reciprocals. Write Yes or No.

1.
$$\frac{3}{4}$$
 and $\frac{4}{3}$

$$\frac{1}{5}$$
 and $\frac{5}{1}$ _____

$$2\frac{3}{4}$$
 and $2\frac{4}{3}$ _____

2. 7 and
$$\frac{7}{1}$$

$$3\frac{2}{5}$$
 and $\frac{5}{17}$ $\frac{9}{10}$ and $\frac{9}{10}$ $\frac{9}{10}$

$$\frac{9}{10}$$
 and $\frac{9}{10}$ _____

Write the reciprocal of each of the following.

$$\boldsymbol{a}$$

$$\boldsymbol{c}$$

3.
$$\frac{5}{6}$$
 ____ 6 ___ 6 ___

4.
$$2\frac{1}{2}$$

$$2\frac{1}{2}$$
 ____ $3\frac{1}{3}$ ____ $1\frac{1}{4}$ ___ $\frac{4}{9}$ ____

$$3\frac{1}{8}$$

5.
$$4\frac{2}{3}$$
 ____ $1\frac{3}{5}$ ____ $\frac{7}{12}$ ____

$$2\frac{13}{16}$$

Lesson 9 Division

To divide by a fraction, multiply by its reciprocal.

Multiply by the reciprocal.

$$\frac{3}{5} \div \frac{1}{2} = \frac{3}{5} \times \frac{2}{1}$$
$$= \frac{6}{5}$$
$$= 1\frac{1}{5}$$

Multiply by the reciprocal.

$$1\frac{3}{5} \div 6 = \frac{\cancel{8}}{5} \times \frac{1}{\cancel{6}}$$
$$= \frac{4}{15}$$

$$\frac{1}{2} \div \frac{3}{4}$$

$$\frac{c}{\frac{4}{5}} \div \frac{8}{15}$$

$$\frac{7}{9} \div \frac{2}{3}$$

2.
$$\frac{7}{8} \div \frac{1}{2}$$

$$\frac{3}{4} \div \frac{1}{8}$$

$$\frac{4}{5} \div \frac{1}{2}$$

$$\frac{2}{3} \div \frac{1}{2}$$

3.
$$8 \div \frac{4}{5}$$

$$2\frac{1}{3} \div 2$$

$$2\frac{2}{5} \div 8$$

$$8\frac{1}{3} \div 10$$

4.
$$5\frac{1}{4} \div \frac{9}{20}$$

$$5\frac{1}{2} \div \frac{1}{4}$$

$$7\frac{3}{4} \div \frac{3}{16}$$

5.
$$10 \div \frac{2}{5}$$

$$1\frac{7}{12} \div \frac{7}{12}$$

$$3\frac{9}{10} \div \frac{13}{15}$$

Lesson 10 Division (mixed numerals) palvios mados at abase 1

 $3\frac{3}{8} \div 1\frac{1}{2} = \frac{27}{8} \div \frac{3}{2}$ Change $3\frac{3}{8}$ and $1\frac{1}{2}$ to improper fractions.

$$=\frac{27}{\cancel{8}}\times\frac{\cancel{2}}{\cancel{3}}$$

 $= \frac{27}{8} \times \frac{2}{3}$ Multiply by the reciprocal of $\frac{3}{2}$.

$$=\frac{9}{4}$$
 or $2\frac{1}{4}$

 $=\frac{9}{4}$ or $2\frac{1}{4}$ Write $\frac{9}{4}$ as a mixed numeral in simplest form.

1.
$$\frac{a}{10} \div \frac{14}{15}$$

$$2\frac{2}{3} \div \frac{2}{3}$$
 $5 \div 1\frac{1}{4}$

$$5 \div 1\frac{1}{4}$$

2.
$$2\frac{1}{3} \div 2\frac{1}{3}$$

$$2\frac{2}{3} \div 3\frac{1}{3}$$

$$2\frac{2}{3} \div 3\frac{1}{3}$$
 $1\frac{2}{5} \div 1\frac{2}{7}$ $2\frac{2}{5} \div 3\frac{1}{3}$

$$2\frac{2}{5} \div 3\frac{1}{3}$$

3.
$$\frac{3}{5} \div 1\frac{2}{7}$$

$$1\frac{1}{8} \div \frac{5}{6}$$

$$1\frac{1}{8} \div \frac{5}{6}$$
 $1\frac{3}{7} \div \frac{5}{7}$ $\frac{1}{2} \div 1\frac{1}{4}$

$$\frac{1}{2} \div 1\frac{1}{4}$$

4.
$$3\frac{1}{3} \div 1\frac{1}{4}$$

$$1\frac{7}{8} \div 1\frac{1}{4}$$

$$1\frac{5}{12} \div 2\frac{2}{3}$$

$$5\frac{3}{5} \div 2\frac{1}{10}$$

Lesson 10 Problem Solving

| 1. | Sean's pool has a leak. It is losing 1L every $\frac{1}{20}$ h. How much water would the pool lose in $\frac{3}{4}$ h? | 1. S 8 S 8 |
|-----|---|---|
| | It would lose L of water. | $\frac{27}{3}$ Mutth |
| 2. | In problem 1, how much water would the pool lose in $2\frac{3}{4}$ h? | 2. |
| | It would lose L of water. | $\frac{1}{4} \text{ or } 2 \frac{1}{4} Worth$ |
| 3. | Mr. Cepuran worked $6\frac{3}{4}$ h giving piano lessons today. Each lesson was $\frac{3}{4}$ h long. How many lessons did he give today? | 3. |
| | He gave lessons. | de la companie de la |
| 4. | Ada, Beth, and Cathy took turns painting the kitchen. They finished in $5\frac{1}{4}$ h. If each girl spent the same amount of time painting, how long did each girl paint? | 4. |
| | Each girl painted for h. | |
| | The girls in problem 4 and a few friends painted the garage next. It took them $7\frac{7}{8}$ h, and they each painted for $1\frac{5}{16}$ h. How many people painted the garage? | 5. |
| | people painted the garage. | |
| 6. | Allen took $1\frac{7}{10}$ h to type $25\frac{1}{2}$ pages. How many pages can he type per hour? | 6. |
| 3 | He can type pages per hour. | |
| | Twenty bags of soil are to be placed in containers. Each container will hold $3\frac{3}{4}$ bags of soil. How many full containers will there be? How much of another container will be filled? | 7. |
| 2.5 | containers will be filled. | |
| | of another container will be filled. | |

Addition and Subtraction Lesson 11

Study how to add or subtract when the denominators are the same. The data at a

Add the numerators.

$$\frac{\frac{2}{9}}{\frac{5}{9}}$$

$$\frac{+\frac{8}{9}}{\frac{15}{9}} \text{ or } 1\frac{2}{3}$$

$$\frac{2}{9} + \frac{5}{9} + \frac{8}{9} = \frac{2+5+8}{9}$$

Use the same
$$=\frac{2}{9}$$
 denominator. $=1\frac{2}{3}$

Subtract the numerators.

$$\frac{\frac{7}{8}}{\frac{3}{8}}$$
Use the same denominator.
$$\frac{\frac{4}{8} \cdot \frac{1}{2}}{\frac{1}{8}}$$

$$=\frac{4}{8}$$

$$=\frac{1}{2}$$

$$\boldsymbol{a}$$

$$\frac{3}{5}$$
 + $\frac{1}{5}$

$$+\frac{6}{8}$$

$$-\frac{\frac{3}{8}}{8}$$

$$\frac{3}{8}$$
 $-\frac{1}{8}$

$$-\frac{9}{10}$$

$$-\frac{1}{10}$$

$$\frac{3}{4}$$

$$-\frac{7}{8}$$

$$-\frac{1}{8}$$

$$\frac{7}{12}$$

$$-\frac{\frac{7}{10}}{\frac{7}{10}}$$

$$\frac{1}{8}$$
 $\frac{3}{8}$ $+\frac{3}{8}$

$$\frac{2}{7}$$
 $\frac{4}{7}$

$$\frac{\frac{7}{10}}{\frac{9}{10}}$$

$$\frac{5}{12}$$
 $\frac{11}{12}$
 $+\frac{11}{12}$

Lesson 11 Problem Solving

| 1. | Lindsay took $\frac{3}{10}$ h to solve a puzzle. Chelsea took $\frac{9}{10}$ h to solve a different puzzle. How much time did the two girls spend on the puzzles in all? | 1. |
|----|--|--------------------------------|
| | They spent h on the puzzles. | |
| 2. | In problem 1, how much longer did Chelsea spend on her puzzle than Lindsay spent on hers? | 2. misaimecab |
| | Chelsea spent h longer on her puzzle. | |
| 3. | Glass A is $\frac{1}{8}$ full, glass B is $\frac{3}{8}$ full, and glass C is $\frac{5}{8}$ full. How many full glasses are there altogether? | 3. |
| | There are full glasses. | taŭ teskinta in awam inni-stat |
| 4. | In problem 3, how much more full is glass C than glass A? | 4. |
| | Glass C is more full. | |
| 5. | In problem 3, how much more full is glass C than glass B? | 5. |
| | Glass C is more full. | |
| 6. | Grant spent $\frac{3}{12}$ h eating, $\frac{11}{12}$ h watching TV, and $\frac{5}{12}$ h reading. How much longer did Grant spend reading than eating? | 6. |
| | He spent h more reading than eating. | |
| 7. | In problem 6, how much longer did Grant spend watching TV than reading? | 7. |
| | He spenth more watching TV than reading. | |
| | In problem 6, how much time did Grant spend in all three activities? | 8. |
| | He spent h. | |

CHAPTER 2

Lesson 12 Equivalent Fractions

You can rename a fraction by multiplying the numerator and the denominator by the same number.

$$\frac{3}{4} = \frac{3}{20}$$

$$\frac{3}{4} = \frac{3 \times 5}{4 \times 5}$$

$$= \frac{15}{20}$$
Choose 5 so the new denominator is 20.

$$4\frac{2}{5} = 4\frac{115}{15}$$

$$4\frac{2}{5} = 4\frac{2 \times 3}{5 \times 3}$$

$$= 4\frac{6}{15}$$
Choose 3 so the new denominator is 15.

Rename.

1.
$$\frac{1}{2} = \frac{1}{16}$$

$$\frac{3}{4} = \frac{1}{12}$$

$$\frac{3}{5} = \frac{3}{15}$$

2.
$$\frac{4}{5} = \frac{10}{10}$$

$$\frac{7}{9} = \frac{7}{45}$$

$$\frac{5}{12} = \frac{3}{36}$$

3.
$$\frac{7}{8} = \frac{7}{24}$$

$$\frac{1}{6} = \frac{1}{30}$$

$$\frac{5}{12} = \frac{1}{60}$$

4.
$$1\frac{2}{3} = 1\frac{2}{6}$$

$$2\frac{5}{8} = 2\frac{1}{40}$$

$$4\frac{1}{4} = 4\frac{1}{8}$$

5.
$$3\frac{8}{9} = 3\frac{1}{18}$$

$$6\frac{7}{10} = 6\frac{1}{60}$$

$$7\frac{5}{6} = 7\frac{24}{24}$$

Addition and Subtraction Lesson 13

To add or subtract when the denominators are different, rename the fractions so the denominators are the same.

The denominators are 4 and 5. Since $4 \times 5 = 20$, rename each fraction with a denominator of 20.

$$\frac{3}{4} \rightarrow \frac{15}{20}$$

$$+\frac{3}{5} \rightarrow +\frac{12}{20}$$

$$\frac{2}{5} \rightarrow \frac{8}{20}$$

$$-\frac{1}{4} \rightarrow -\frac{5}{20}$$

$$\frac{3}{20} \rightarrow +\frac{1}{2} \rightarrow +1$$

$$+1\frac{1}{2} \rightarrow +1$$

$$4$$
Write answers in simplest form.

The denominators are 2 and 3. Since $2 \times 3 = 6$, rename each number with a denominator of 6.

Write each answer in simplest form.

 \boldsymbol{a}

$$\boldsymbol{b}$$

 \boldsymbol{c}

1.

$$+\frac{1}{3}$$

$$\frac{7}{8} + \frac{1}{3}$$

d

$$+\frac{\frac{1}{2}}{\frac{2}{3}}$$

2.

$$-\frac{2}{3}$$
 $-\frac{1}{5}$

$$-\frac{7}{8}$$

$$-\frac{3}{4}$$
 $-\frac{2}{3}$

3.

$$3\frac{5}{8} + 2\frac{4}{5}$$

$$4\frac{1}{2} + 1\frac{2}{3}$$

$$5\frac{2}{3} + 2\frac{3}{10}$$

4.

$$5\frac{1}{5}$$

$$-2\frac{1}{6}$$

$$4\frac{3}{4}$$
 $-4\frac{2}{3}$

$$7\frac{4}{5}$$
 $-6\frac{7}{12}$

CHAPTER 2

Lesson 14 Addition and Subtraction

When one denominator is a factor of the other, use the greater denominator as the common denominator.

2 is a factor of 10, so use 10 as the common denominator.

$$\frac{\frac{7}{10}}{+\frac{1}{2}} \rightarrow \frac{\frac{7}{10}}{+\frac{5}{10}} + \frac{3\frac{1}{2}}{\frac{1}{10}} \rightarrow \frac{3\frac{5}{10}}{+\frac{3}{10}} + \frac{3\frac{5}{10}}{\frac{1}{10}} \rightarrow \frac{1\frac{3}{10}}{4\frac{8}{10}} = 4\frac{4}{5}$$

3 is a factor of 6, so use 6 as the common denominator.

$$\frac{\frac{2}{3}}{-\frac{1}{6}} \rightarrow \frac{\frac{4}{6}}{-\frac{1}{6}} \rightarrow \frac{4\frac{5}{6}}{-\frac{1}{6}} \rightarrow \frac{1\frac{2}{3}}{-\frac{1}{6}} \rightarrow \frac{1\frac{4}{6}}{3\frac{1}{6}}$$

$$\boldsymbol{a}$$

1.
$$\frac{1}{2}$$
 + $\frac{3}{4}$

$$\frac{7}{8} + \frac{3}{4}$$

$$\frac{8}{9}$$

$$\frac{2}{3} + \frac{1}{12}$$

2.
$$3\frac{2}{5} + 1\frac{7}{20}$$

$$6\frac{11}{16} + 3\frac{1}{2}$$

$$+7\frac{7}{24}$$

 $+4\frac{5}{6}$

$$5\frac{1}{4} + 2\frac{5}{12}$$

3.
$$\frac{9}{10}$$
 $-\frac{1}{2}$

$$-\frac{5}{6}$$
 $-\frac{1}{3}$

$$-\frac{7}{8}$$

$$-\frac{1}{2}$$

$$-\frac{\frac{3}{4}}{\frac{7}{16}}$$

4.
$$2\frac{5}{6}$$
 $-1\frac{2}{3}$

$$6\frac{5}{8}$$

$$-3\frac{1}{4}$$

$$5\frac{4}{5}$$
 $-2\frac{9}{20}$

$$9\frac{11}{24}$$
 $-7\frac{3}{8}$

Lesson 14 Problem Solving

Stock Market Report for McTavish Dog Supplies (changes given in dollars)

| Monday | Tuesday | Wednesday | Thursday | Friday |
|------------------|---------|-------------------|----------|--------|
| $up \frac{7}{8}$ | up 3/4 | up $1\frac{1}{2}$ | up 2 7/8 | |

| 1. | How much greater was Monday's gain than Tuesday's? | 1. <u>8</u> [+ | |
|----|--|------------------|------------------|
| | Monday's gain was dollars greater. | | |
| 2. | What was the combined gain for Monday and Tuesday? | 2. | 3. |
| | The combined gain was dollars. | ero) saeloniz qi | rawena doue atur |
| 3. | What was the combined gain for Wednesday and Thursday? | d | 3 |
| | The combined gain was dollars. | | |
| 4. | The price before trading Monday was $23\frac{5}{8}$ dollars. What was the price after Monday's trading? | 4. | 5. |
| | The price was dollars. | | |
| 5. | The price after Thursday's trading was $29\frac{5}{8}$ dollars. The price after Friday's trading was $26\frac{1}{2}$ dollars. How much did the stock go down on Friday? | | |
| | It went down dollars. | | |
| | A recipe for punch calls for $\frac{3}{4}$ L orange juice and $\frac{2}{3}$ L cranberry juice. How much more orange juice does the recipe call for than cranberry juice? | 6. | 7. |
| | The recipe calls for L more orange juice. | | |
| | $2\frac{1}{2}$ L of water is poured into a jug with a mass of $2\frac{9}{10}$ kg. The water has a mass of $2\frac{1}{2}$ kg. What is the combined mass of the water and the jug? | | |
| | The combined mass is kg. | | |

Lesson 15 Addition and Subtraction

The denominators 4 and 10 have a common factor of 2. Use $(4 \times 10) \div 2$ or 20 as the common denominator.

The denominators 8 and 12 have a common factor of 4. Use $(8 \times 12) \div 4$ or 24 as the common denominator.

$$\frac{\frac{3}{4} \rightarrow \frac{15}{20}}{+\frac{7}{10} \rightarrow +\frac{14}{20}} \qquad 2\frac{\frac{9}{10} \rightarrow 2\frac{18}{20}}{+\frac{3\frac{1}{4}}{20} \rightarrow +\frac{3\frac{5}{20}}{20}} \\
+\frac{3}{10} \rightarrow +\frac{14}{20} \qquad +\frac{3\frac{1}{4}}{20} \rightarrow +\frac{3\frac{5}{20}}{20} \\
5\frac{23}{20} = 6\frac{3}{20}$$

$$\begin{array}{c}
\frac{7}{8} \to \frac{21}{24} \\
-\frac{5}{12} \to -\frac{10}{24} \\
\frac{11}{24}
\end{array}$$

$$6\frac{11}{12} \to 6\frac{22}{24} \\ -2\frac{5}{8} \to -2\frac{15}{24} \\ 4\frac{7}{24}$$

CHAPTER 2

Write each answer in simplest form.

 \boldsymbol{a}

$$\frac{1}{6} + \frac{3}{8}$$

b

$$\frac{3}{4} + \frac{1}{6}$$

C

$$\frac{3}{10} + \frac{4}{15}$$

a

2.
$$1\frac{3}{4}$$

1.

$$3\frac{7}{15}$$
 + $2\frac{1}{6}$

$$4\frac{11}{12}$$

$$8\frac{3}{6} + 4\frac{7}{10}$$

3.
$$\frac{1}{4}$$
 $-\frac{1}{6}$

$$\frac{8}{9}$$
 $-\frac{5}{6}$

$$-\frac{7}{12}$$
 $-\frac{3}{16}$

$$-\frac{13}{25}$$
 $-\frac{7}{15}$

4.
$$2\frac{5}{6}$$
 $-1\frac{1}{4}$

$$6\frac{11}{15}$$
 $-3\frac{7}{10}$

$$9\frac{1}{8}$$
 $-5\frac{1}{10}$

$$8\frac{17}{20}$$
 $-2\frac{5}{12}$

Lesson 15 Problem Solving

Solve. Express each answer in simplest form.

| 1. | . Matthew worked $\frac{5}{6}$ h on Monday, $\frac{3}{4}$ h on Tuesday, and $\frac{9}{10}$ h on Wednesday. How many hours did he work on Monday and Tuesday? | 1. mones muses | |
|---------|---|------------------|----------------------|
| | He worked h on Monday and Tuesday. | 10 20 | |
| 2. | In problem 1, did Matthew work longer on Monday or Wednesday? How much longer did he work on that day? | 2. | 3. 0 <u>0</u> |
| | He worked longer on | | |
| | He worked h longer. | anel sasquine at | Aveta equi sonsve |
| 3. | In problem 1, how many hours did Matthew work on Tuesday and Wednesday? | ő | |
| | He worked h on these two days. | | 3 |
| 4. | June solved the first math problem in $\frac{9}{16}$ min, the second problem in $1\frac{7}{8}$ min, and the last problem in $1\frac{3}{4}$ min. How long did it take her to solve the first and third problems? | 4. | 5. |
| - Obres | It took her min to solve the first and third problems. | 8 | |
| 5. | In problem 4, which problem took June longer to solve, the second problem or the third problem? How much longer did it take? | | |
| | The problem took her longer. | | |
| | It took her min longer. | | |
| 6. | On a test, Brenda worked $\frac{7}{30}$ h, Emma worked $\frac{7}{20}$ h, and Laura worked $\frac{7}{15}$ h. Which girl worked the least amount of time? How long did the other two girls work on the test? | 6. | 7. |
| | worked the least amount of time. | -8 | |
| | The other girls worked h. | | |
| 7. | In problem 6, how long did Brenda and Emma work on the test? | | |
| | They worked h | | |

Lesson 16 Subtraction (renaming)

To subtract, rename 6 as 54.

To subtract, rename $4\frac{5}{15}$ as $3\frac{20}{15}$.

$$\begin{array}{c}
4\frac{1}{3} \\
-1\frac{3}{5}
\end{array}
\xrightarrow{4\frac{5}{15}}
\xrightarrow{4\frac{5}{15}}
\xrightarrow{73\frac{20}{15}}
\xrightarrow{-1\frac{9}{15}}
\xrightarrow{2\frac{11}{15}}$$

$$4\frac{5}{15} = 3 + 1 + \frac{5}{15}$$
$$= 3 + \frac{15}{15} + \frac{5}{15}$$
$$= 3\frac{20}{15}$$

CHAPTER 2

Write each answer in simplest form.

a

b

C

d

1. $7 - \frac{7}{2}$

 $9 - \frac{3}{10}$

 $\frac{6}{3\frac{1}{2}}$

 $4\frac{2}{7}$ $-2\frac{6}{7}$

2. $4\frac{1}{4}$ $-2\frac{1}{2}$

 $4\frac{2}{3}$ $-1\frac{4}{5}$

 $6\frac{1}{2}$ $-1\frac{3}{8}$

 $1\frac{1}{3}$ $-\frac{1}{2}$

3. 2 $-\frac{3}{4}$

 $3\frac{1}{2}$ $-1\frac{2}{3}$

 $\frac{6}{-1\frac{5}{6}}$

 $7\frac{1}{8}$ $-4\frac{5}{6}$

4. $5\frac{2}{3}$ $-\frac{5}{6}$

 $4\frac{2}{15} \\ -3\frac{7}{10}$

 $7\frac{5}{9}$ $-4\frac{7}{12}$

 $8\frac{3}{4}$ $-3\frac{4}{5}$

Lesson 16 Problem Solving

| Rehearsal Schedule | |
|--------------------|-----------------|
| Day | Time |
| Monday | 2 h |
| Tuesday | 1 5/6 h |
| Wednesday | $\frac{3}{4}$ h |
| Thursday | $1\frac{3}{5}h$ |
| Friday | |



2.

Solve each problem.

1. How many hours less did the group practise on 1. Wednesday than on Monday?

They practised _____ h less on Wednesday.

2. How much longer did they practise on Tuesday than on Thursday?

They practised _____ h longer on Tuesday.

3. Find the combined practice time for Wednesday and Thursday.

The combined practice time was _____ h.

4. Find the average time they practised on Wednesday and Thursday.

The average time was _____ h.

5. On Friday they practised twice as long as they practised on Wednesday. How long did they practise on Friday?

They practised _____ h on Friday.

3.

4.

5.

CHAPTER 2 PRACTICE TEST Operations Involving Fractions

1.
$$\frac{2}{3} \times \frac{2}{3}$$

$$\frac{4}{5} \times \frac{5}{6}$$

$$\frac{3}{10} \times \frac{8}{9}$$

$$\frac{1}{2} \times \frac{3}{10} \times \frac{8}{9}$$
 $\frac{1}{2} \times \frac{2}{3} \times \frac{3}{4}$



2.
$$12 \times 7\frac{1}{2}$$

$$1\frac{4}{5} \times 3\frac{1}{3}$$

$$\frac{8}{9} \times 7\frac{1}{2}$$

$$1\frac{4}{5} \times 3\frac{1}{3}$$
 $\frac{8}{9} \times 7\frac{1}{2}$ $4 \times 3\frac{1}{2} \times 2\frac{3}{4}$

3.
$$\frac{4}{5} \div \frac{5}{6}$$

$$\frac{7}{8} \div \frac{3}{10}$$

$$12 \div 1\frac{1}{8}$$

$$12 \div 1\frac{1}{8}$$
 $4\frac{2}{3} \div 1\frac{1}{6}$

4.
$$\frac{2}{5}$$
 + $\frac{2}{5}$

$$\frac{7}{9} + \frac{2}{3}$$

$$3\frac{3}{4} + 4\frac{1}{3}$$

$$\frac{5}{6}$$
 + 2 $\frac{3}{10}$

5.
$$\frac{9}{10}$$

$$-\frac{6}{7}$$
 $-\frac{3}{8}$

$$7
-2\frac{1}{4}$$

$$3\frac{2}{5}$$

$$-1\frac{7}{10}$$